

THEORETICAL SUMMARY

1. What is the quark-gluon plasma?

First principle calculations

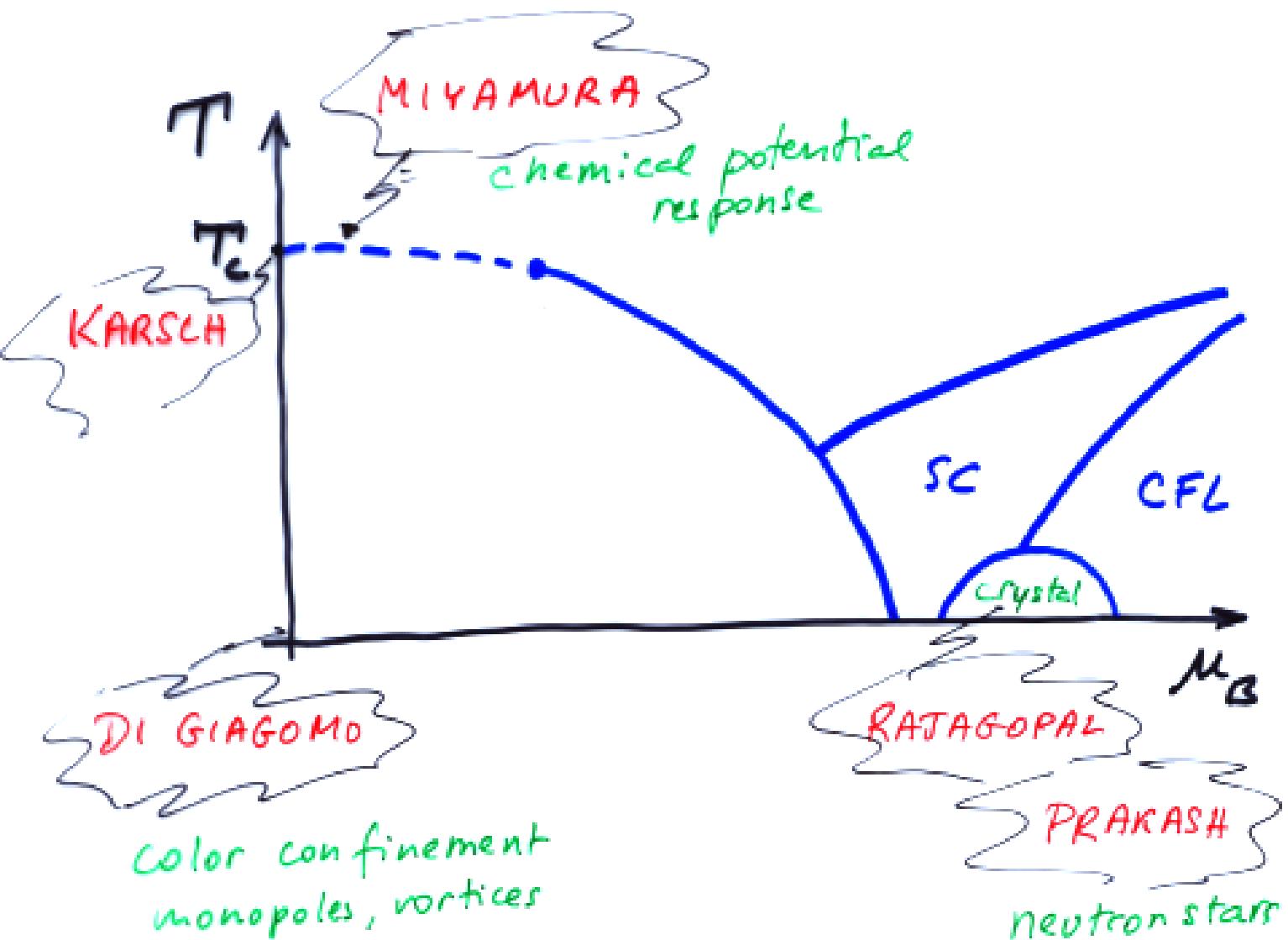
2. Nucleus-nucleus collisions. The standard picture

- Freeze out and hadronization
- Models and degrees of freedom
- Initial conditions

3. Specific signals /observables

- Fluctuations
- Elliptic flow
- Strangeness
- Dileptons
- $T/4$

THE PHASE DIAGRAM



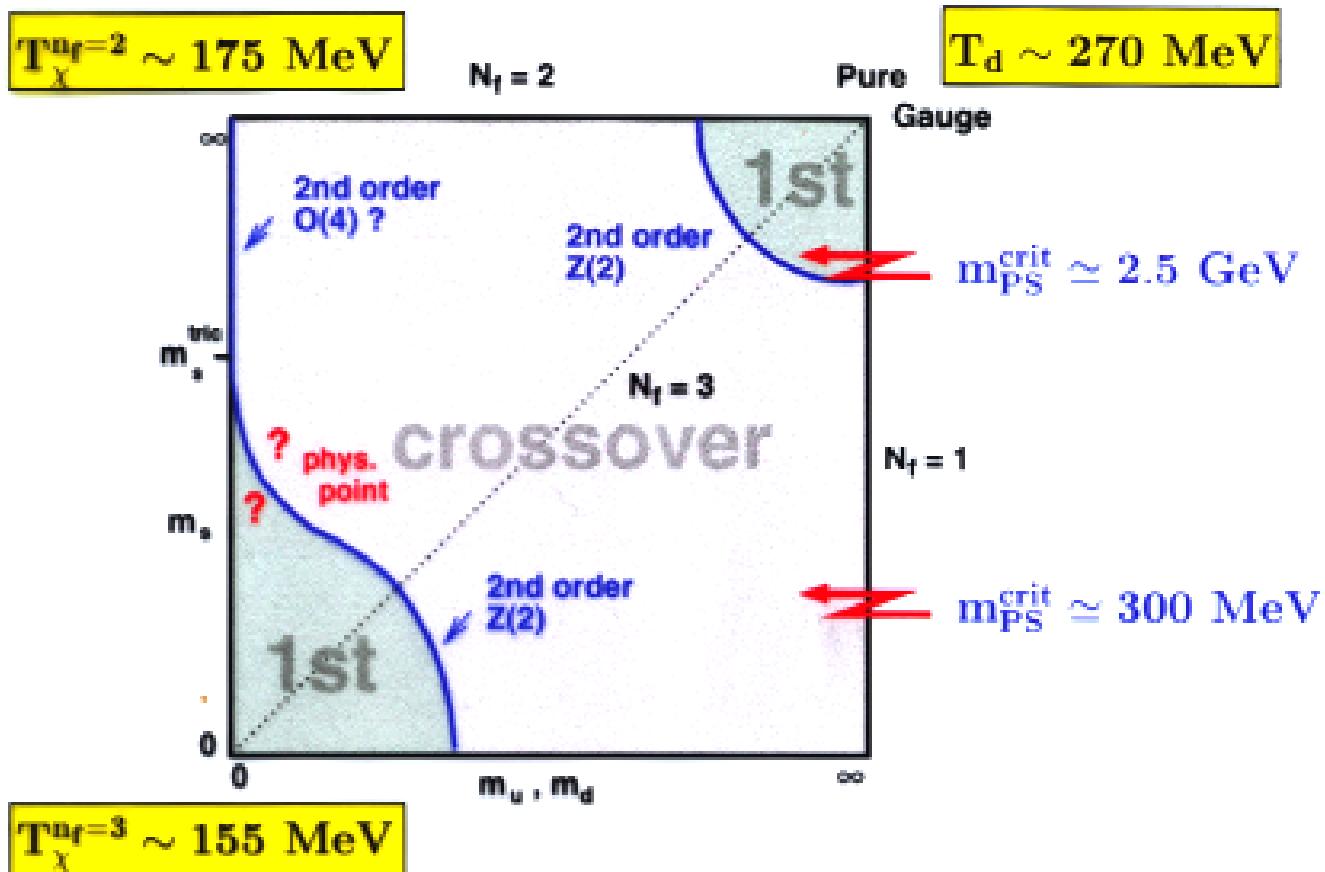
II) QCD (phase) transition temperature

new results:

Clover-fermions ($\mathcal{O}(a)$ improved WF): CP-PACS, hep-lat/0008011v3
 rot. sym. improved SF (p4-action): Bielefeld, hep-lat/0012023

- global symmetries control order of the transition for
 - $m_q \rightarrow \infty \Rightarrow$ deconfinement transition
 - $m_q \rightarrow 0 \Rightarrow$ chiral transition
- rapid crossover in ϵ/T^4 ; peaks in susceptibilities define transition temperatures for all m_q

3-flavor phase diagram



- How to compare QCD calc. with varying m_q and n_f ?
 ⇒ assume exp. value for m_ρ^{nr} (or $\sqrt{\sigma}$) for all n_f

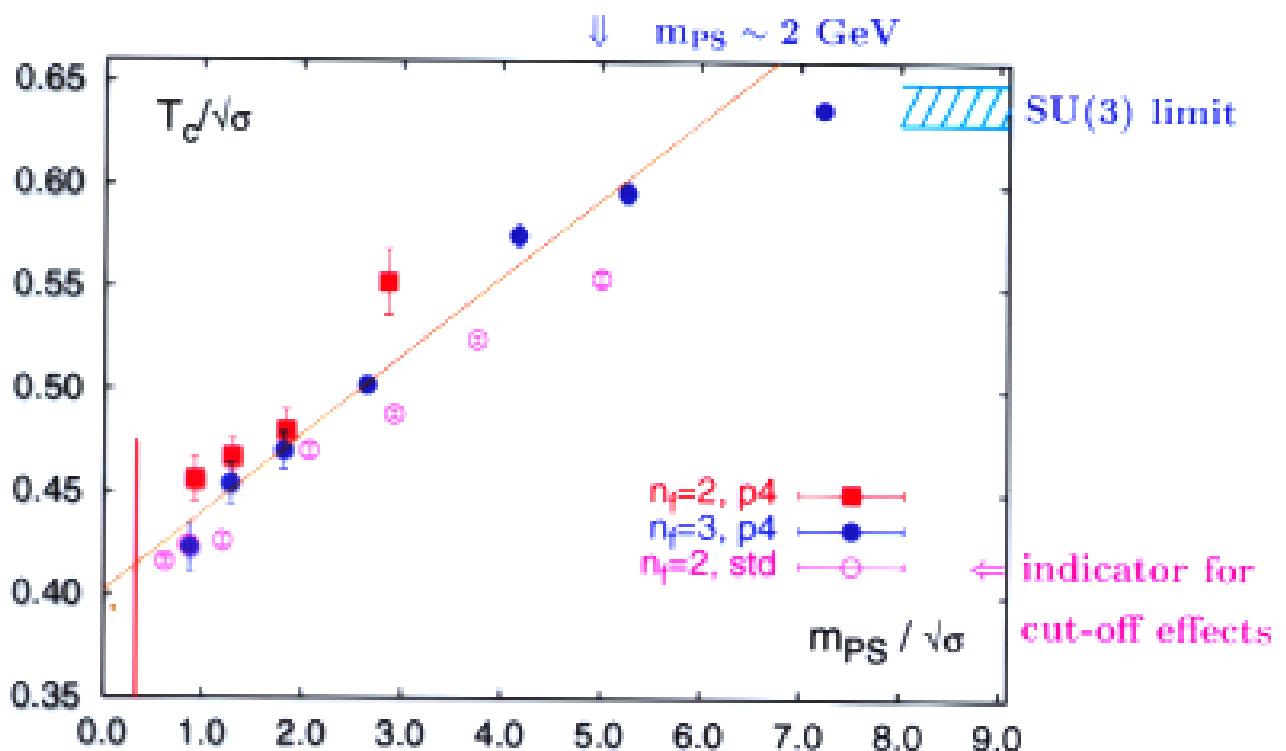
Quark Mass Dependence of T_c

need a m_q (and n_f) independent observable to set a scale

$$\frac{\sqrt{\sigma}}{m_\rho} = \begin{cases} 0.552(13) & , \text{ quenched } (m_q \rightarrow \infty) \\ 0.532(18) & , \text{ partially quenched, } m_q = 0.1, n_f = 3 \\ 0.53(3) & , \text{ chiral limit, } n_f = 3 \end{cases}$$

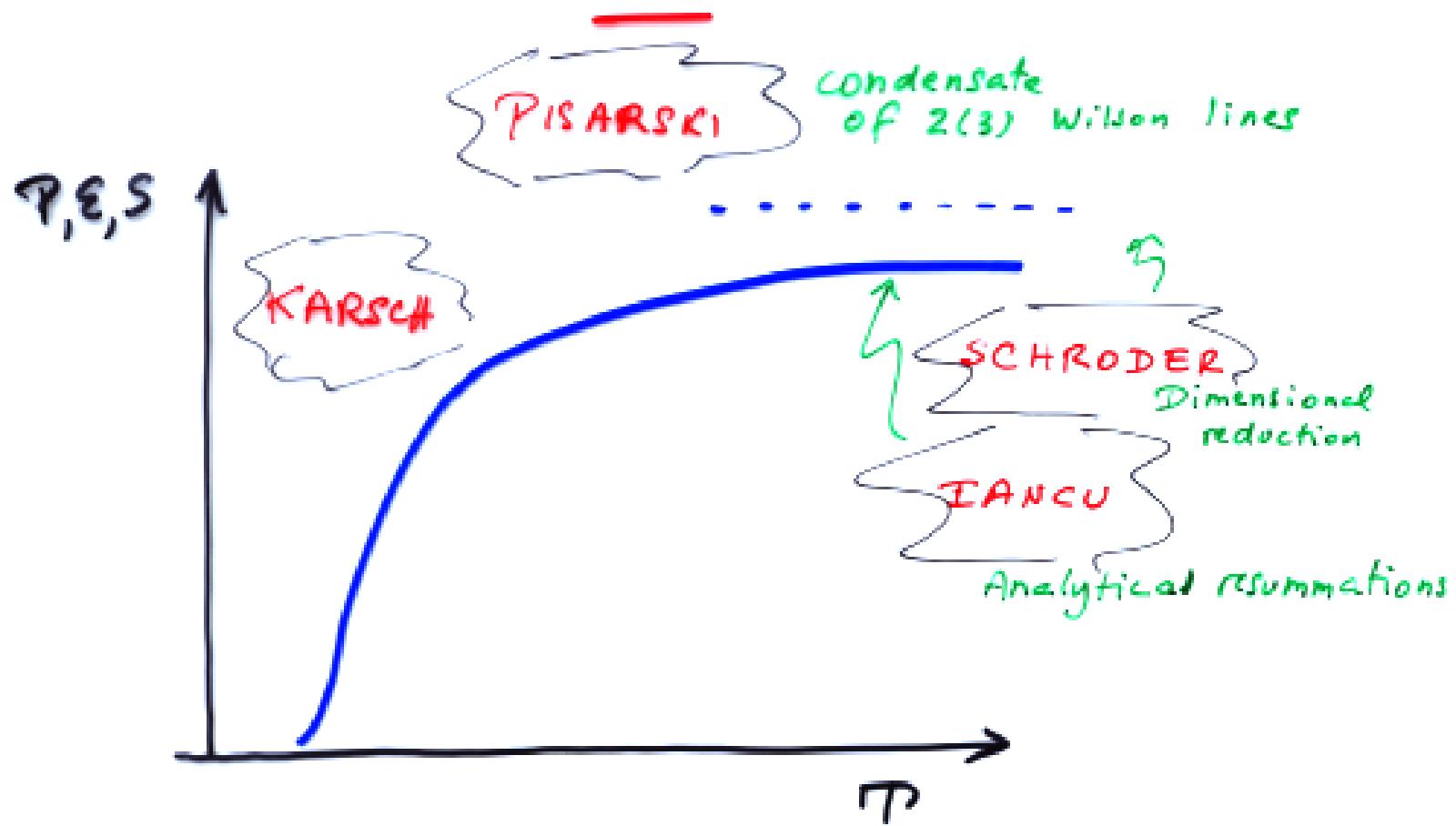
$\Rightarrow \sqrt{\sigma}$, quenched hadron masses are good scale parameters

$$T_c(m_{PS}) \simeq T_c(0) + 0.04(1)m_{PS}$$

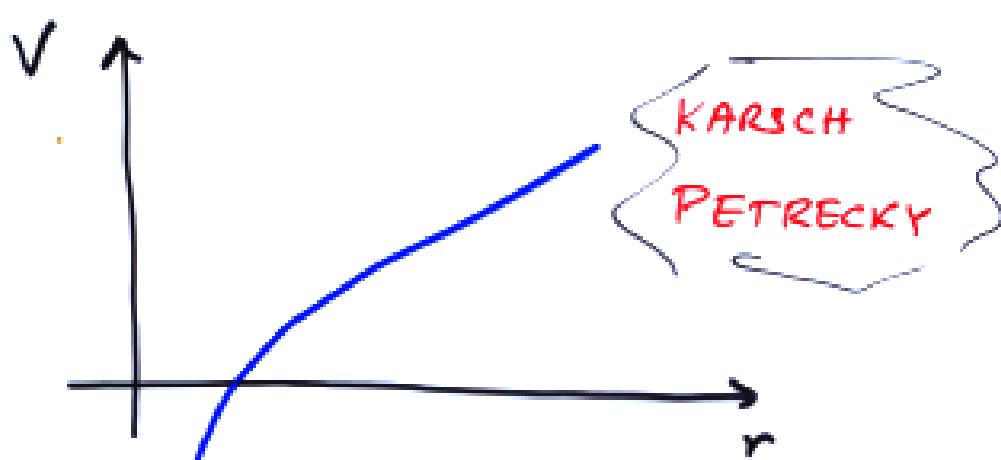


- weak quark mass dependence of $T_c/\sqrt{\sigma}$
 \Rightarrow gross features of the transition not controlled by “light” mesons

EQUATION OF STATE

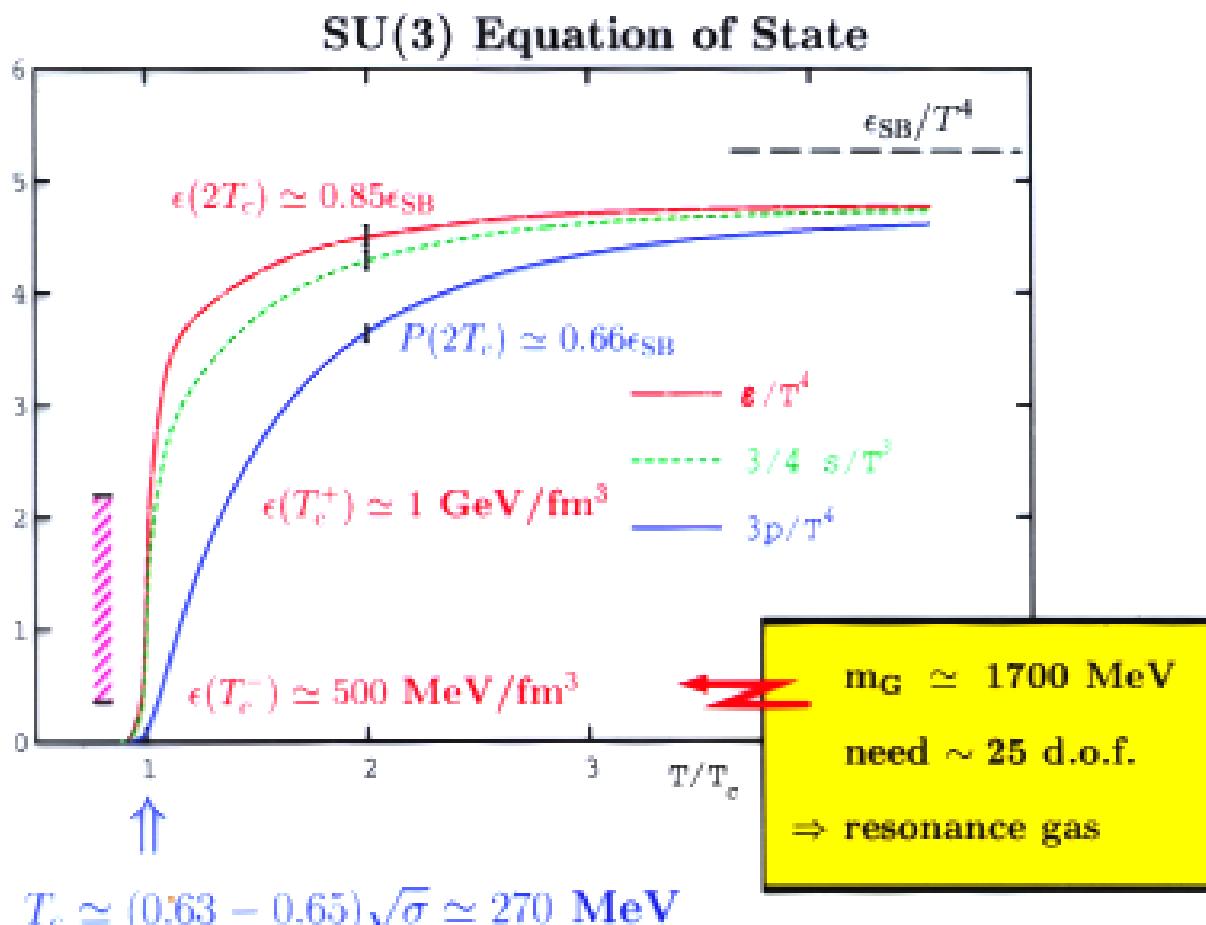


HEAVY QUARK POTENTIAL



III) QCD-EoS and critical energy density

- $\epsilon_{\text{SB}} \sim T^4 \Leftrightarrow (\text{relevant momenta}) \sim T$
 - EoS is sensitive to short distance physics
 - Lattice calculations sensitive to cut-off effects
- experience gained in the pure gauge sector
 - improved actions mandatory
 - EoS non-perturbative even at $T \simeq 5T_c$



high-T behaviour can be reproduced in continuum approaches
(HTL-resummed perturbation theory, quasi-particle models)

- J.O. Andersen et al., PR D61 (2000) 014017;
- J.-P. Blaizot, et al., PRL 83 (1999) 2906; PL B470 (1999) 181
- P. Lévai and U. Heinz, PR C57 (1998) 1879

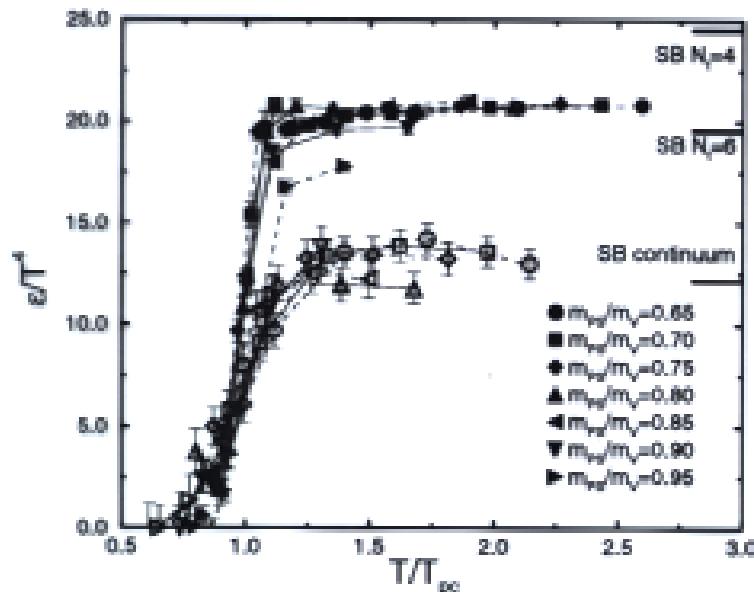
parallel session: E. Iancu, R. Pisarski, Y. Schroder
poster P037: R. Peslier

Energy Density

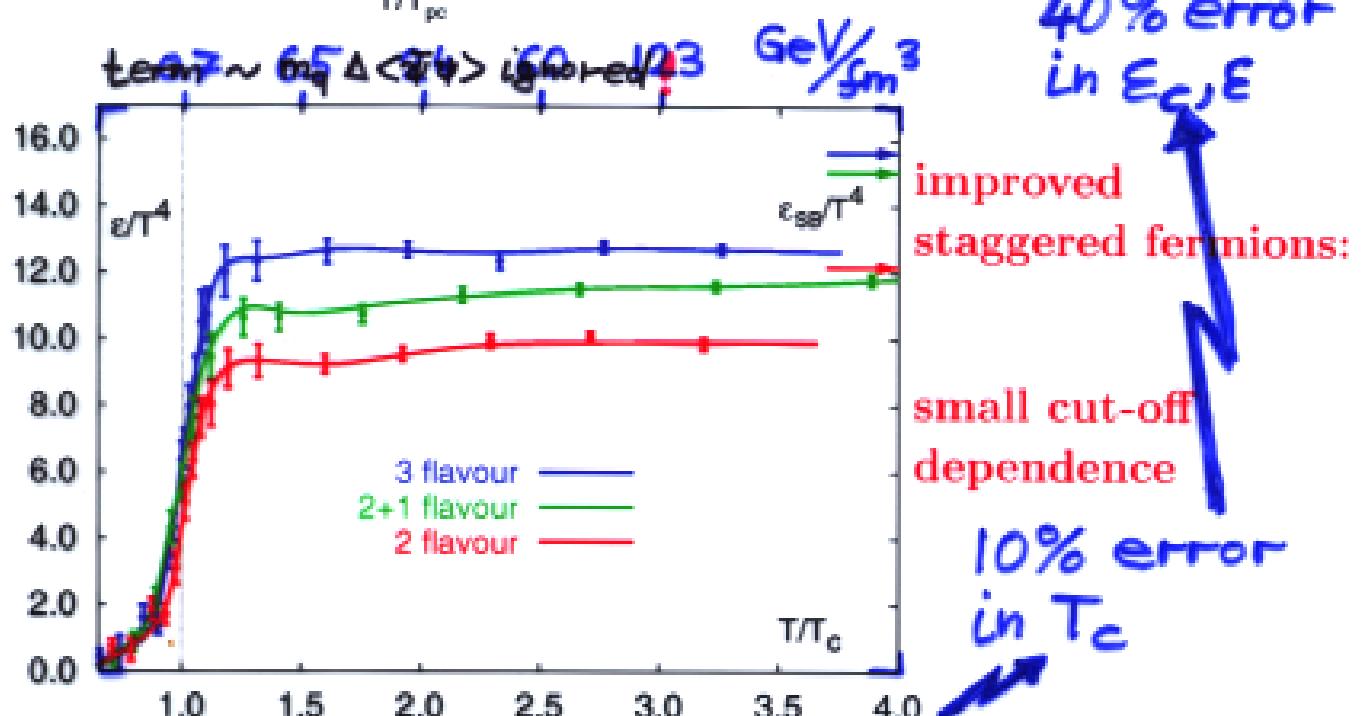
new results:

Clover improved WF (CP-PACS in prep.), S. Ejiri, hep-lat/0011006v2
 rot. sym. improved SF (Bielefeld):

A. Peikert et al., Phys. Lett. B478 (2000) 447



$n_f = 2$ Clover fermions:
 large cut-off dependence
 for $T > T_c$



$$\text{critical energy density: } \epsilon_c \simeq (6 \pm 2) T_c^4$$

even massless pions would contribute only 10% to this!

detailed analysis of volume and quark mass dependence still needed!

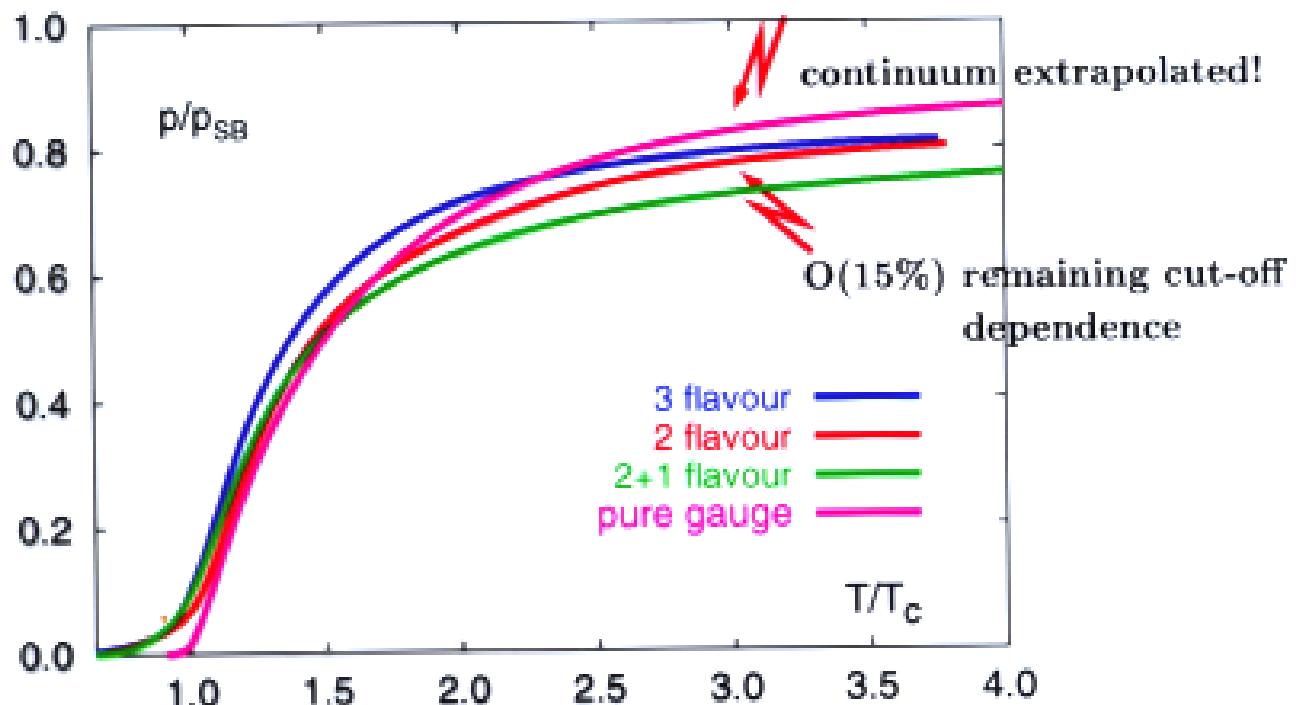
Flavor (IN)-dependence of the EoS

N
↓

flavor dependence dominated by ideal gas term

$$\frac{p(n_f, T)}{T^4} \simeq \left(16 + \frac{7}{8} \cdot 12n_f \right) \frac{\pi^2}{90} f(T)$$

heavy quark contribution is slightly suppressed relative to a massive ideal gas with $m/T \simeq 1$



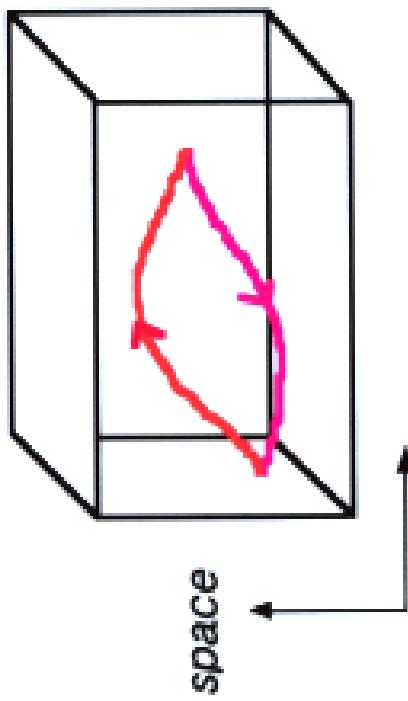
quark mass independence
examined for $n_f = 4$
and also for WF

Hadronic correlations in lattice QCD

- Traditional tool : asymptotic analysis

$$D(\tau) = \int_{\tau \rightarrow \infty} \langle H(\tau, \vec{x}) H(0) \rangle d^3x \sim e^{-m\tau}$$

$T=0$



MEM $\Rightarrow P[A|D]$

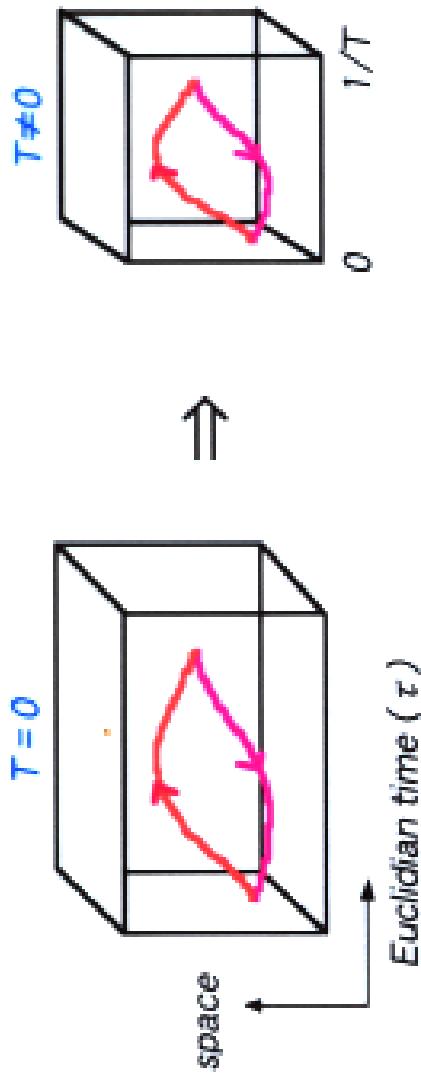
- (i) No parametrization of $A(\omega)$
- (ii) unique solution for $D(\tau) \rightarrow A(\omega)$
- (iii) Statistical significance of $A(\omega)$

Asakawa, Nakahara & T.H.,
PRD (98), hep-lat/0011040
— MELQCD Collaboration —

- New approach : Maximal Entropy Method (MEM)

$$D(\tau) = \int_0^\infty e^{-\omega\tau} A(\omega) d\omega \quad (\text{use all } \tau)$$

Hadronic correlations at finite T in lattice QCD

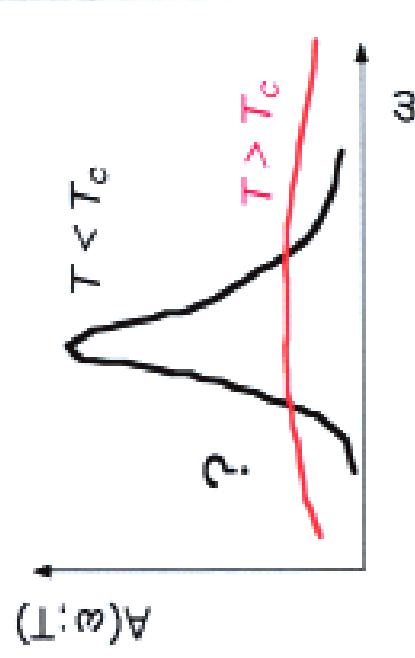


$$D(\tau; T) = \int_0^\infty \frac{e^{-\omega\tau} + e^{+\omega(\tau - 1/T)}}{1 - e^{-\omega/T}} A(\omega; T) d\omega$$



Lattice QCD + MEM provides a clue
to study in-medium hadrons (ρ , J/Ψ , ...)

$$\langle \bar{q} q \rangle_A$$

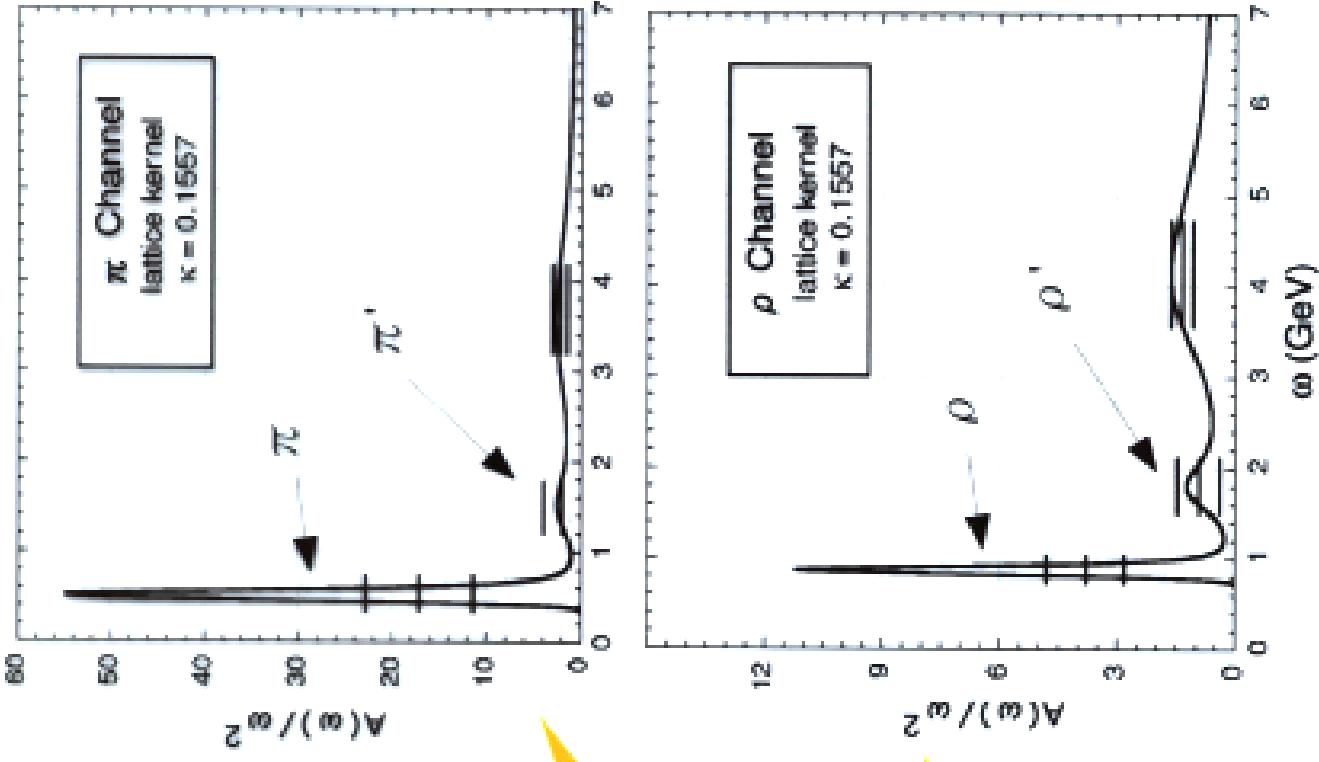
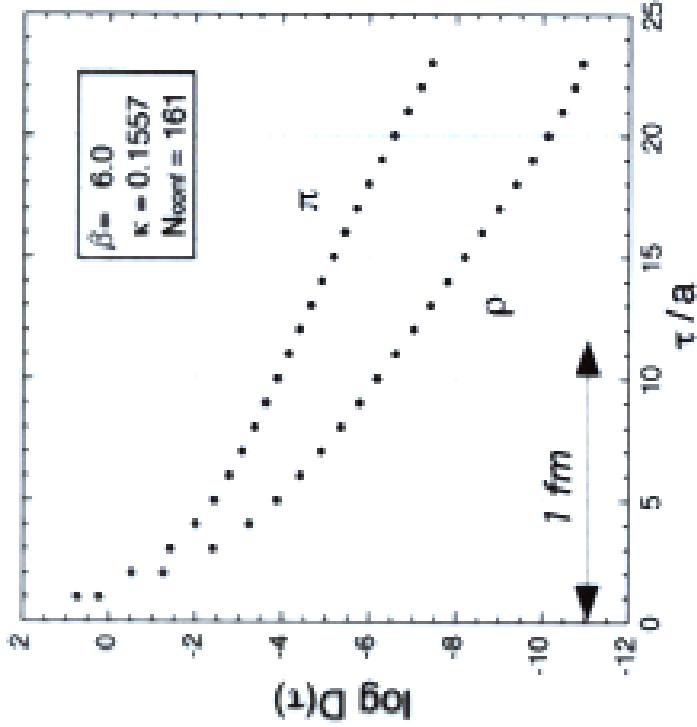


preliminary studies are started:
Asakawa, Nakahara & T.H., in progress.
Oewers, Davies & Shigemitsu, hep-lat/0009031.
Wetzorke & Karsch, hep-lat/0008008.

[$32^3 \times 32, \Lambda_B, 64, \beta = 7.0; \alpha_s/\alpha_S = 1/4$ on CP-PACS]

Spectral functions in π & ρ channels at $T = 0$

quenched approximation
lattice size: $20^3 \times 24$



MEM

Asakawa, Nakahara & T.H., PRD (99), hep-lat/0011040

— MELSCD Collaboration —

THE STANDARD PICTURE

HADRONIZATION and FREEZE-OUT

D. RISCHKE

K. REDLICH

MODELS and DEGREES OF FREEDOM

S. BASS

K. ESKOLA

INITIAL CONDITIONS

R. VENUGOPALAN

D. SON

HADRONIZATION and FREEZE-OUT

- Apparent chemical equilibrium
Particle ratios are functions
of T and μ_B only.

(D. Rischke, K. Redlich, L. Bravina)

- In-medium modifications
of hadrons may modify
freeze out parameters

(D. Rischke, GE Brown)

Statistical-Thermal Models

- At freeze-out: the available particle phase space is occupied according to statistical laws
-> thermal distribution
- Chemical freeze-out: particle abundances are frozen in
- Thermal freeze-out: particle spectra are frozen in

Test of equilibration required to specify:

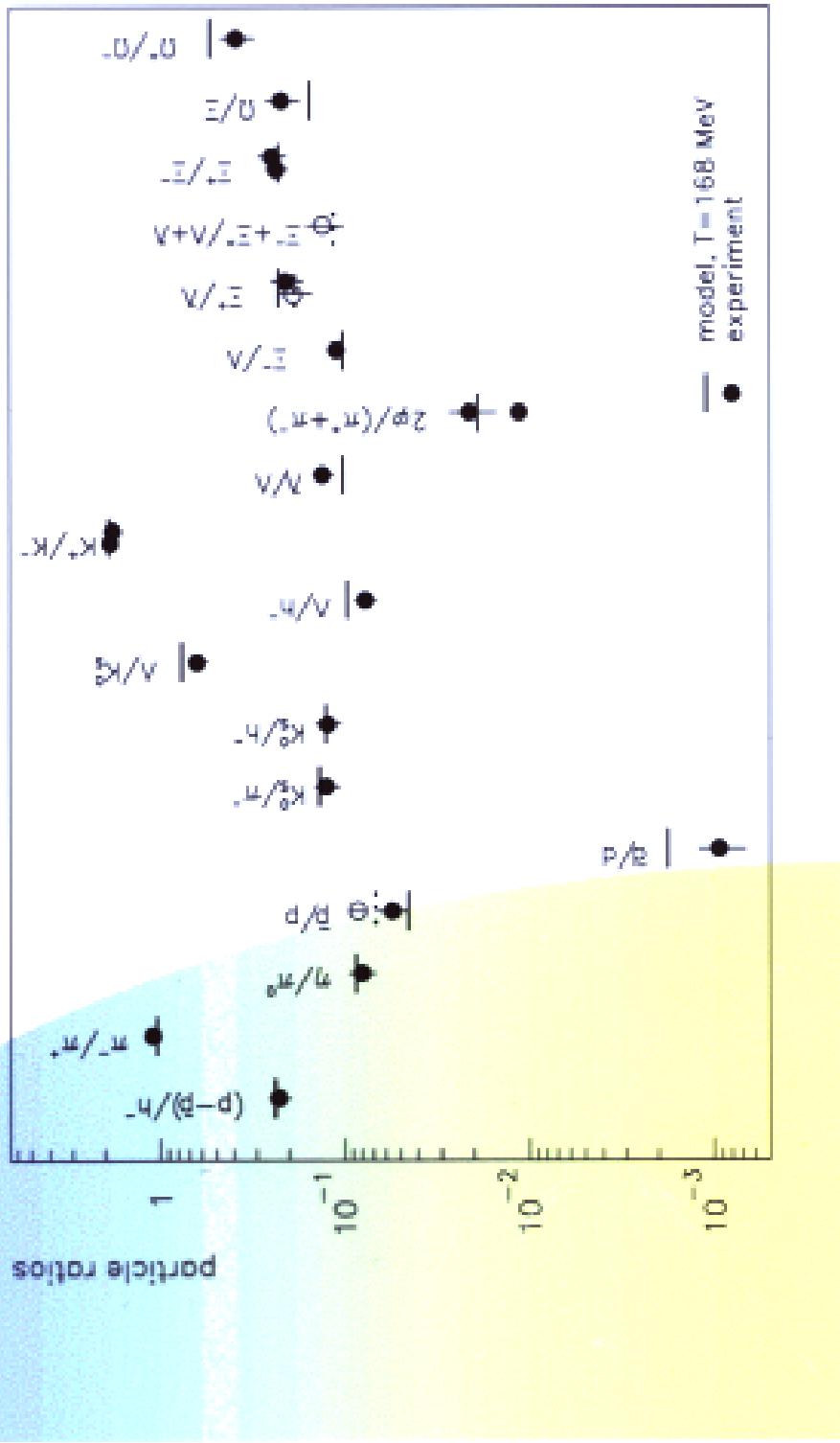
- i) level of observation: (multiplicities, spectra, correlations,...)
- ii) Statistical operator:

$$Z^{GC}(T, \vec{\mu}, V) = Tr[e^{-\beta(H - \mu_B B - \mu_S S - \mu_Q Q)}]$$

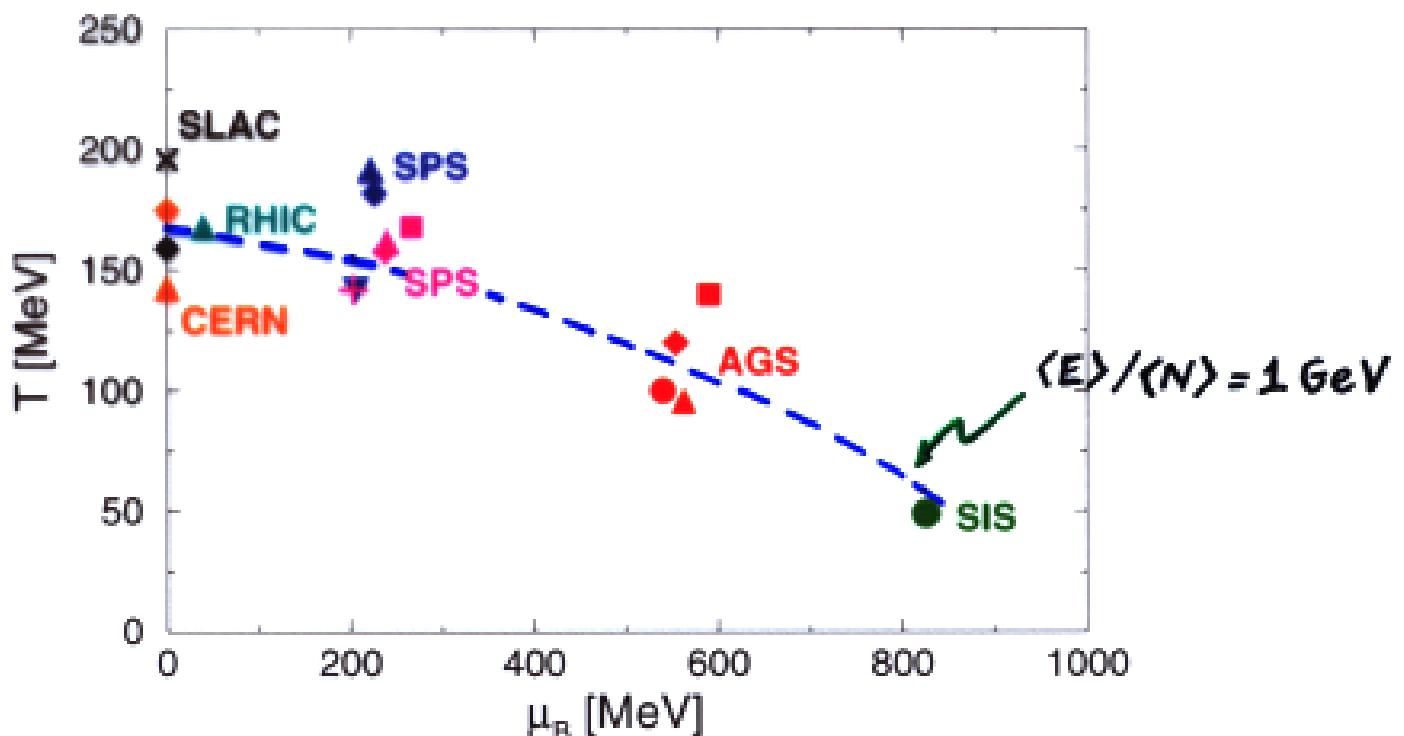
Test of chemical equilibrium for Pb-Pb at SPS

P. Braun-Munzinger, I. Heppe, J. Stachel

$$\varepsilon \approx 0.6 \text{ GeV} / \text{fm}^3, \rho_B \approx 0.16 / \text{fm}^3$$



T, μ_B at freeze-out from particle ratios:



Au+Au, 2.3 AGeV

● [1] Cleymans et al., PRC 59 (99) 1663

← Exact charge
conservation

■ [2] Yen et al., JPG 24 (98) 1777

← exact. volume

◆ [3] Becattini et al., hep-ph/0002267

← $\gamma_s < 1$

▲ [4] Kabana et al., hep-ph/0010247

← $\gamma_s = 1$

● [5] Cleymans et al., PLB 388 (96) 5

◆ [6] Becattini, JPG 23 (97) 1933

← hydro

▼ [7] Sollfrank, EPJC 9 (9) 159

← hydro

▲ [8] Panagiotou et al., PRC 53 (96) 1353

■ [9] Braun-Munzinger et al., PLB 465 (9) 15

S+S, 20 AGeV

◆ [3]

Pb+Pb, 17 AGeV

▲ [4]

Au+Au, 130 AGeV

+ [10] Letessier et al., IJMPE 9 (00) 107

← $\gamma_s > 1$

▲ [4]

◆ [11] Becattini et al., ZPC 74 (97) 319

p-pbar, 900GeV

▲ [4]

e+e-, 29GeV

× [12] Hoang et al., ZPC 38 (88) 603

← fit to $E \frac{d\sigma}{dp}$

◆ [13] Becattini et al., hep-ph/0010221

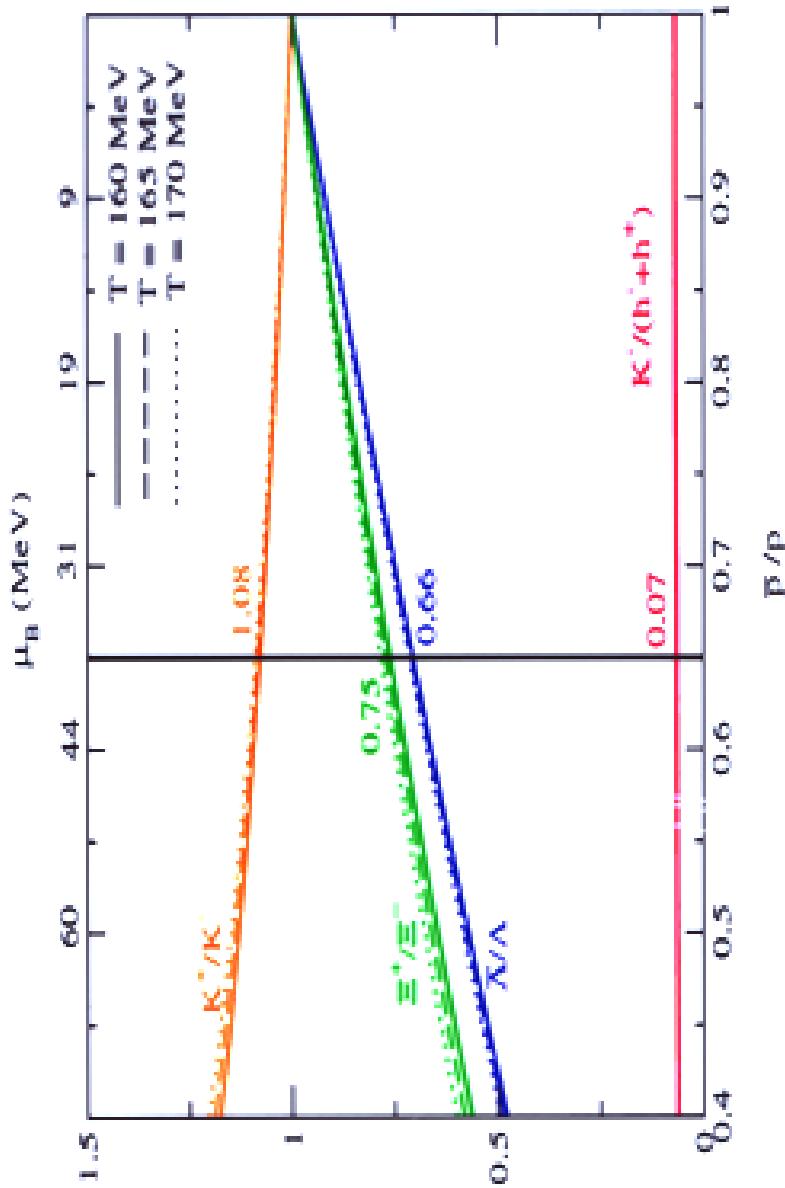
Cf. also: J. Sollfrank, J. Phys. G 23 (97) 1903

J. Cleymans, K. Redlich, PRC 60, 054908 (99)

Thermal Model at RHIC

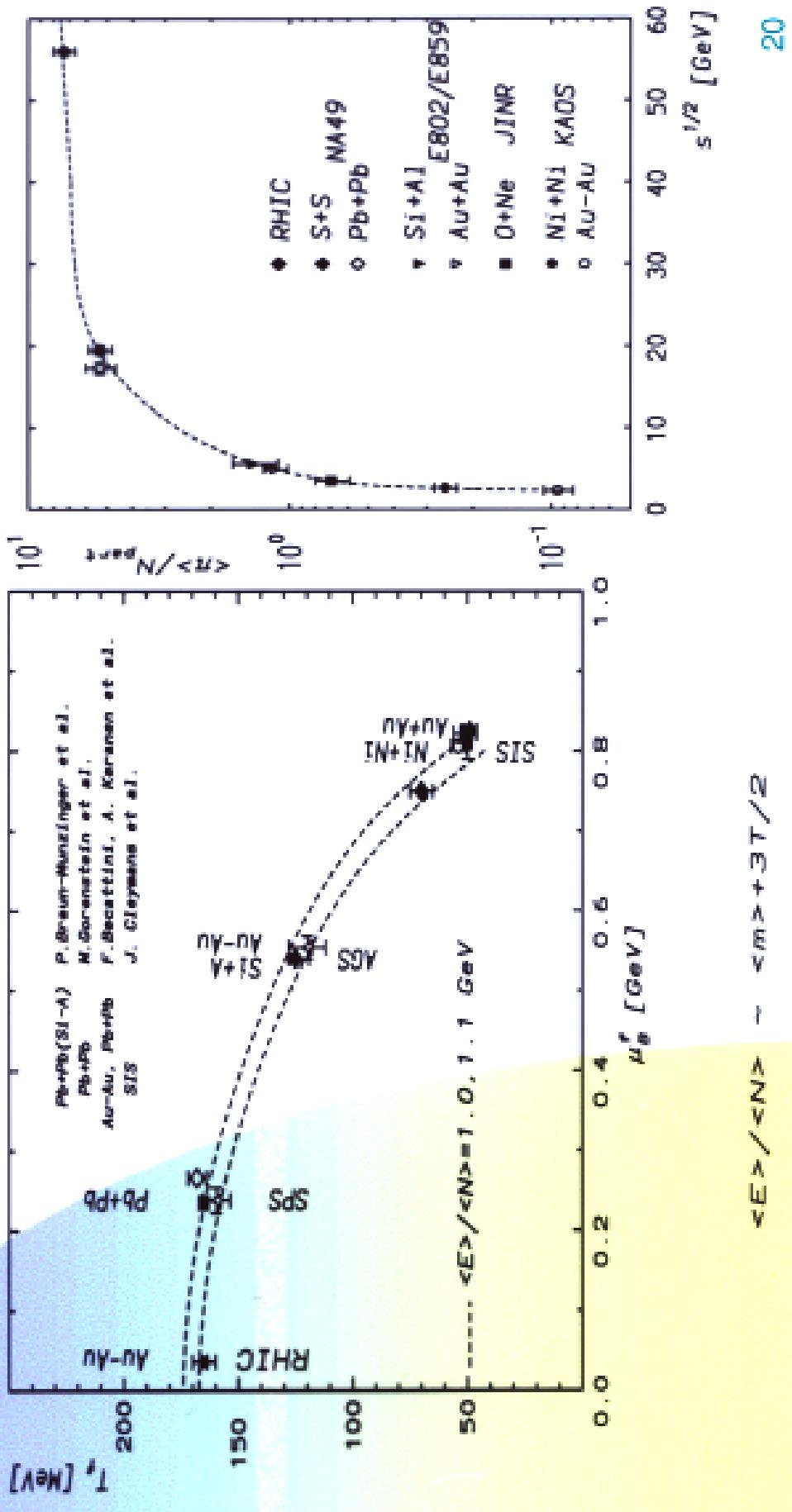
F. Becattini, J. Cleymans, A. Keranen, E. Suhonen, K. R

10



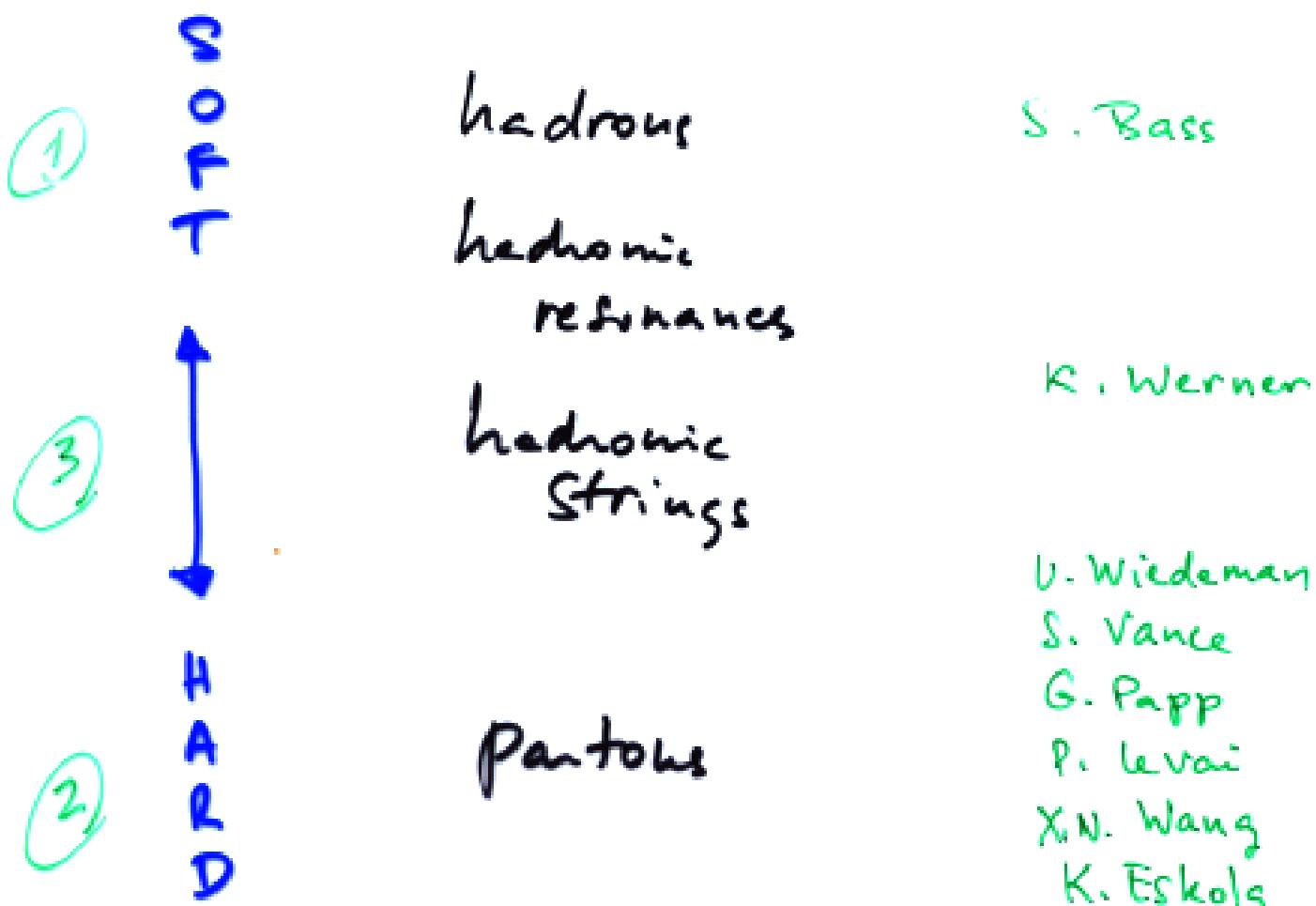
Unified freeze-out curve from SIS => RHIC

J. Cleymans, K.R.



Models and degrees of freedom

- No single model for the entire collision process → various models best suited for different stages of the reaction



Some quotations :

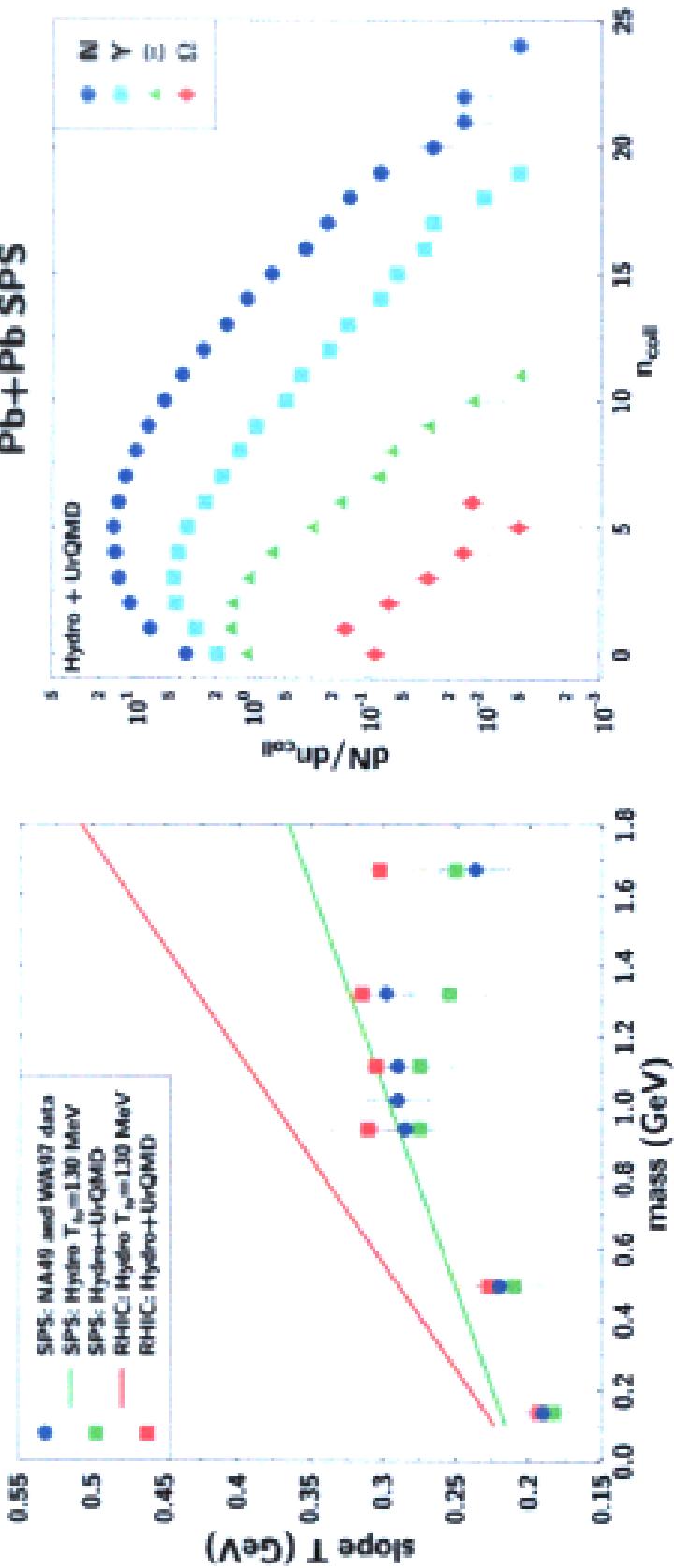
"Theoretical uncertainties
are bigger than experimental
error bars"

(K. ESKOLA)

"We have to be more
concerned about the theoretical
content of models : an
ill-defined model which
fits the data is quite
useless"

(K. WERNER)

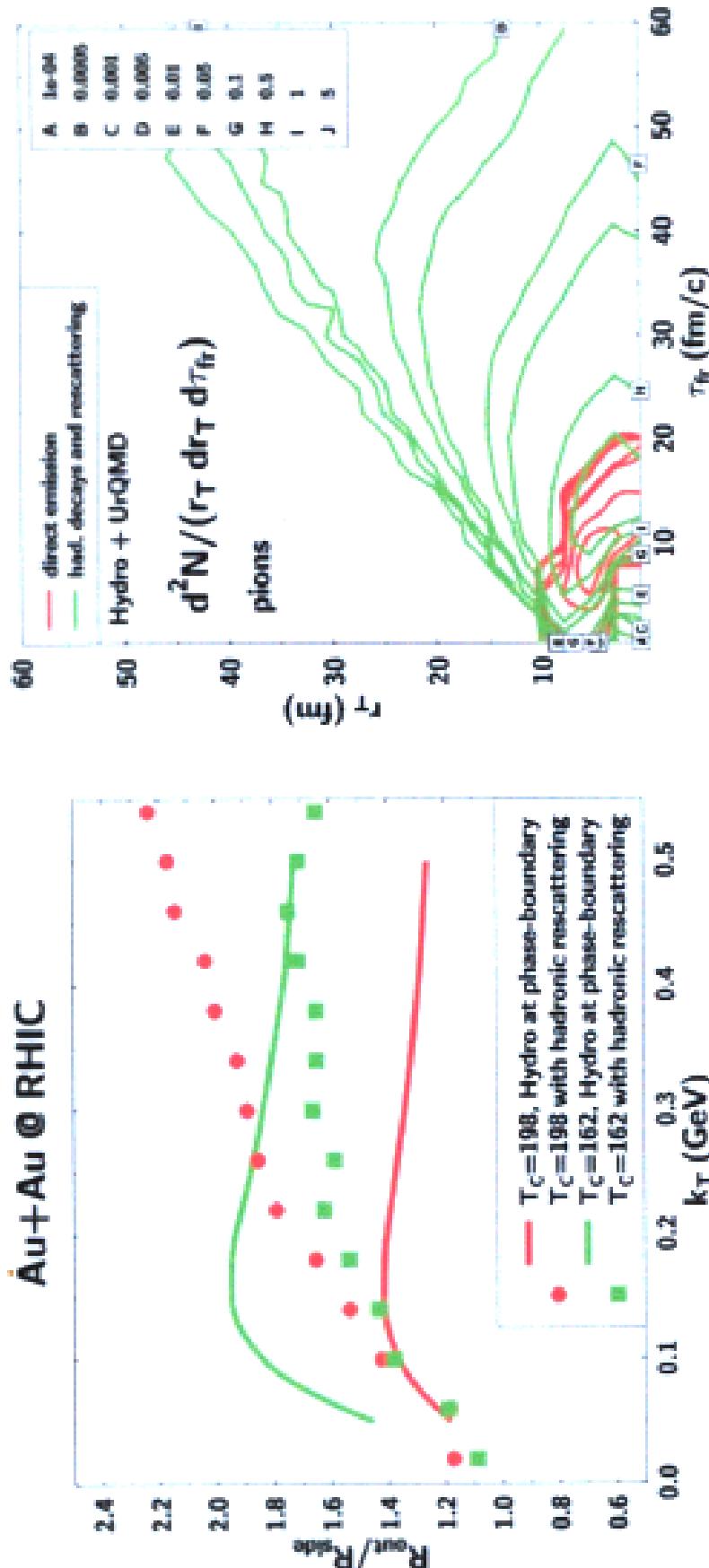
Flavor Dynamics: Radial Flow



- **Hydro:** linear mass-dependence of slope parameter, strong radial flow
- **Hydro+Micro:** softening of slopes for multistrange baryons
 - early decoupling due to low collision rates
 - nearly direct emission from the phase boundary

HBT: QGP Lifetime vs. Hadronic Halo

Au+Au @ RHIC



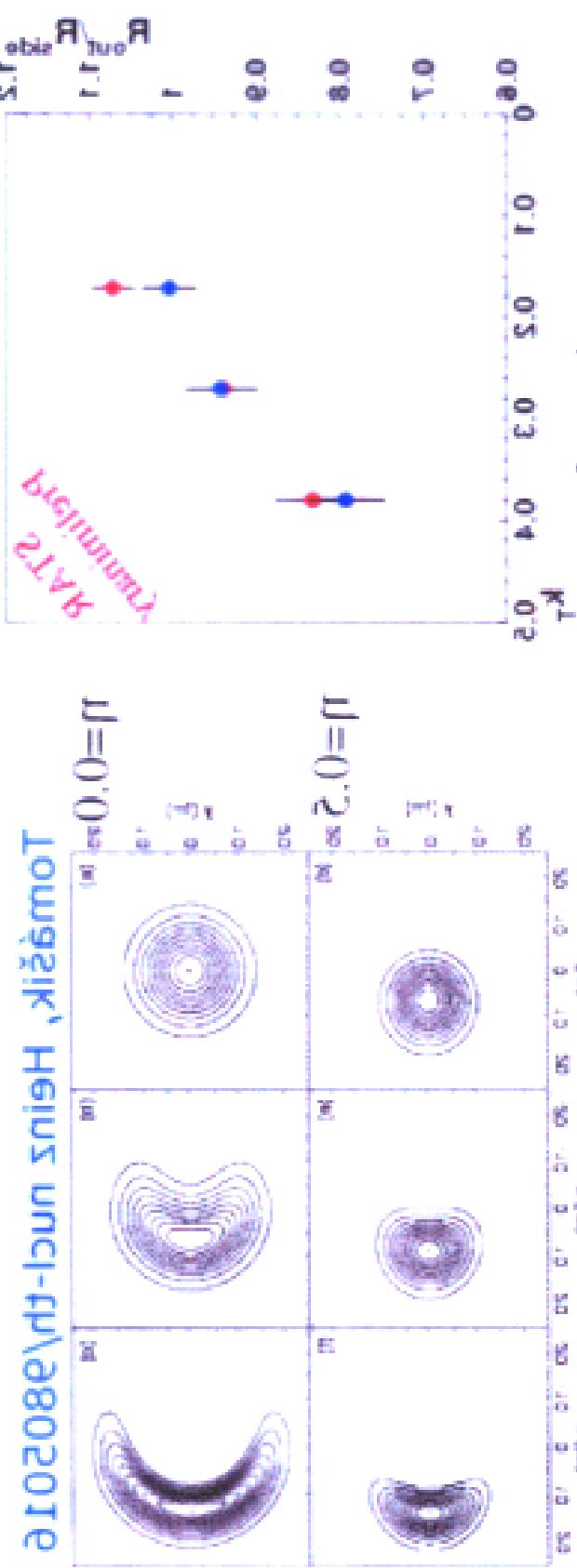
- large R_{out}/R_{side} has been proposed as indicator of long-lived QGP
- inclusion of hadronic phase: only weak sensitivity to initial conditions
 - long-lived dissipative hadronic phase dominates correlation signal
 - dissipative hadronic phase: unavoidable consequence of thermalized QGP

the homogenous field dependence (independence) of the
x-b correlation (wave)

Note: extreme long wave in KHC

observing

$$\kappa^1 = (b_1^1 + b_2^1) \sqrt{2}$$

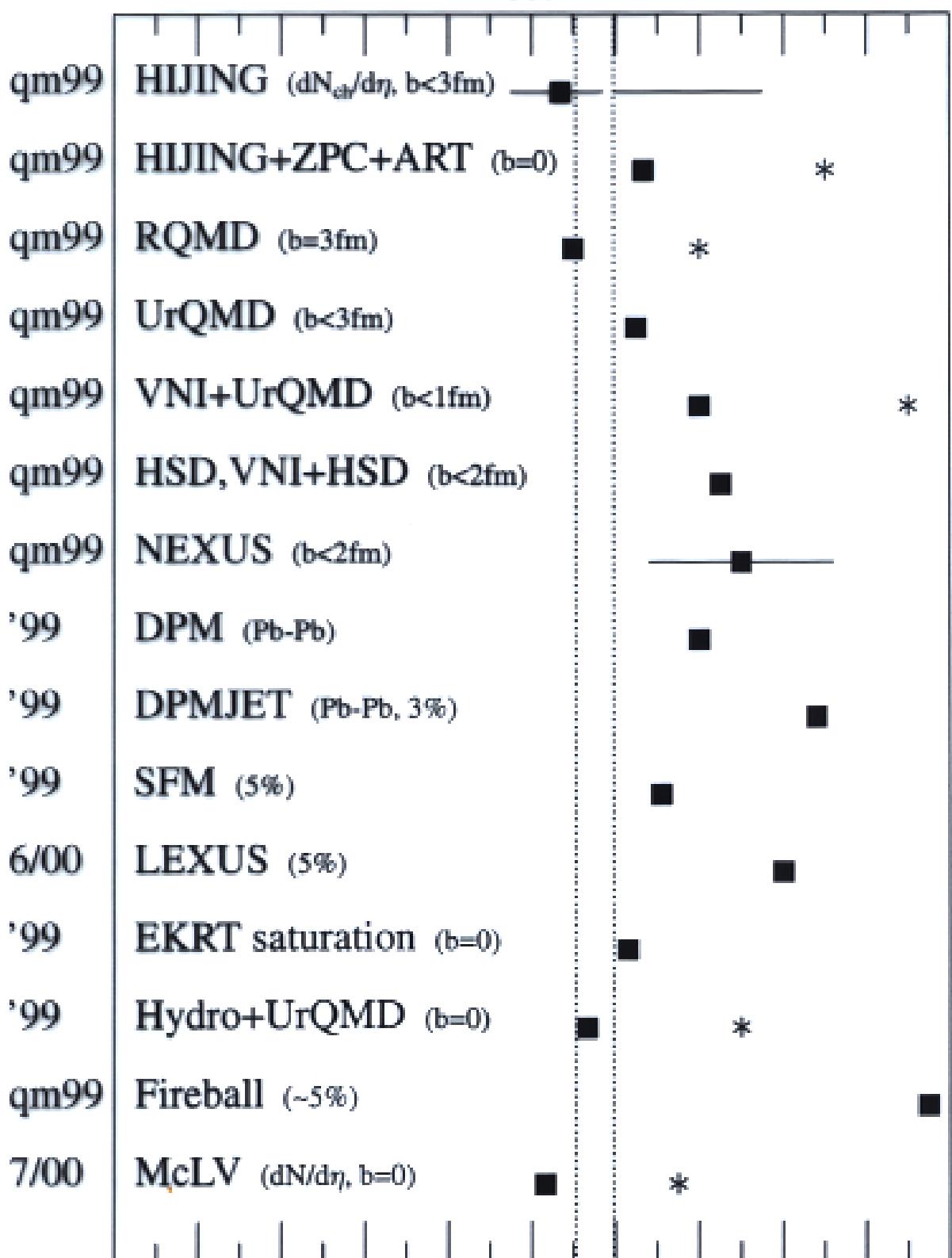


connection between source: $I = \sqrt{K^{opt}_1 - K^{opt}_2} / \sqrt{B^1}$

The K^{opt}_1/K^{opt}_2 Ratio

dN_{ch}/dy , Au+Au, $y=0$, $s^{1/2}=200 \text{ AGeV}$

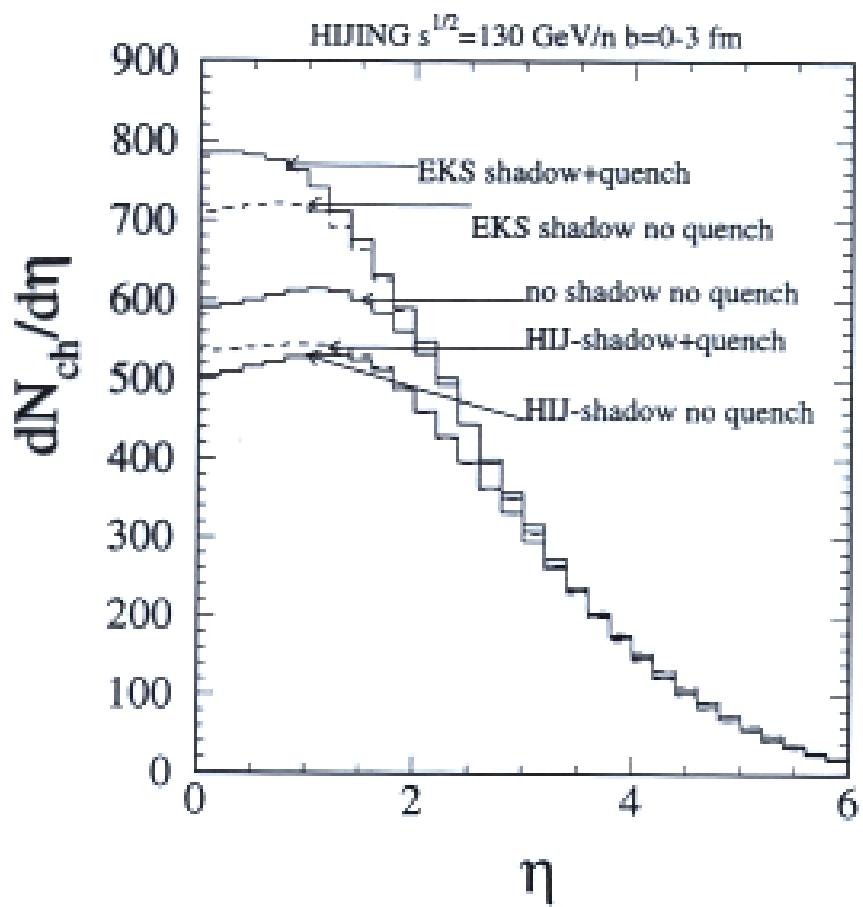
600 800 1000 1200 1400 1600



Applied $\sim \frac{2}{3}$: $N(*) \rightarrow N_{ch}$ data * $(200/130)^{0.37} * 1.1$

Net $\begin{cases} \sim 1.1 : & \eta \rightarrow y \\ \sim 0.9 : & b = 0 \rightarrow b \lesssim 3 \text{ fm}(5\%) \end{cases}$

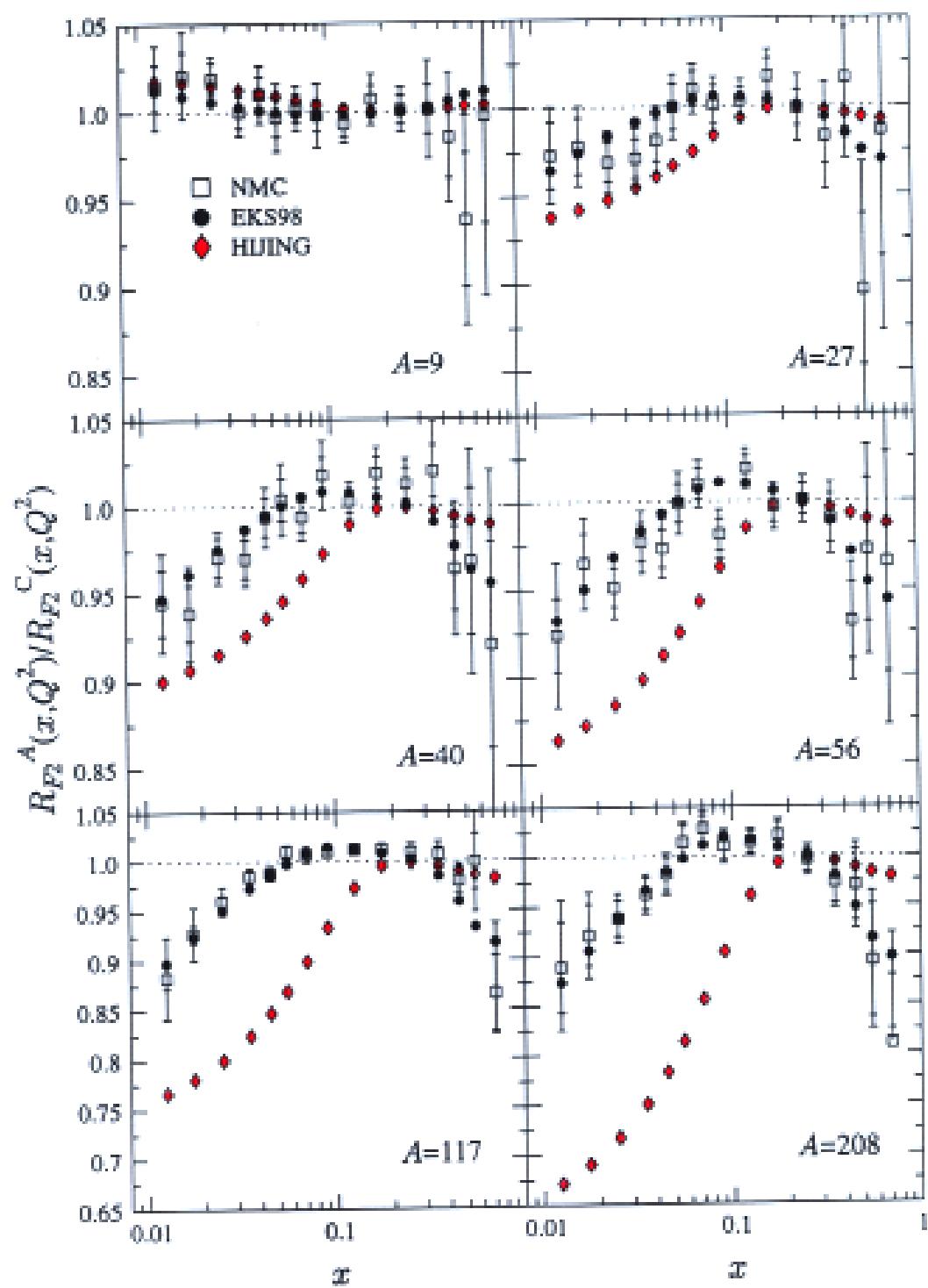
see [Armesto,Pajares, hep-ph/0002163]



HIJING prediction, from X.-N. Wang

EKS98 = DGLAP + constraints from DIS & DY,
conservation of B & p

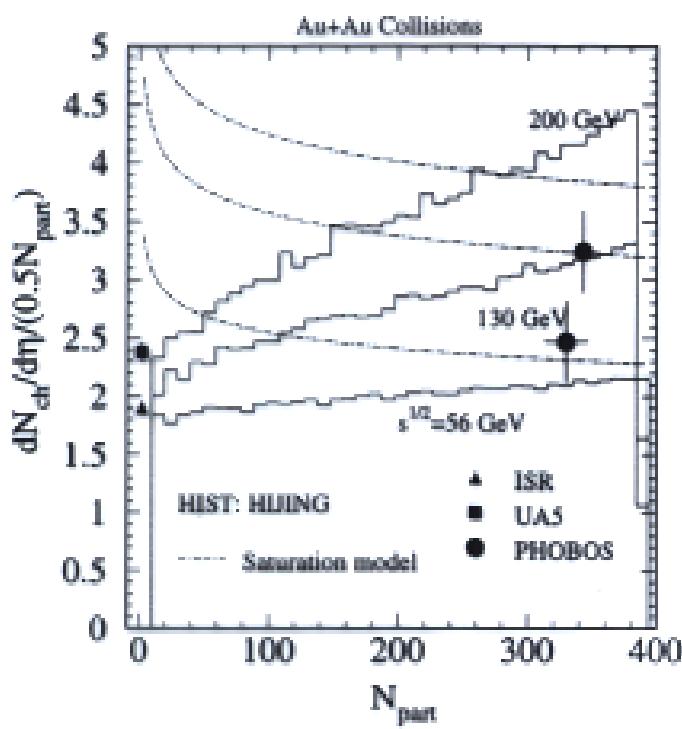
[Eskola, Kolhinen, Salgado, hep-ph/9807297]



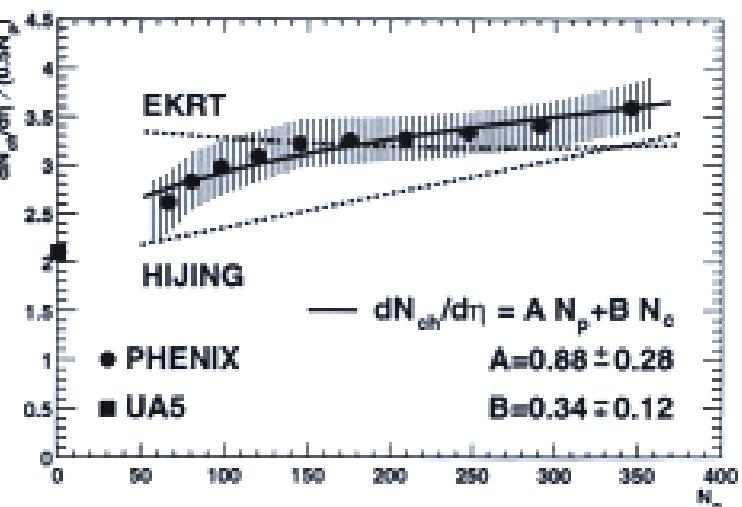
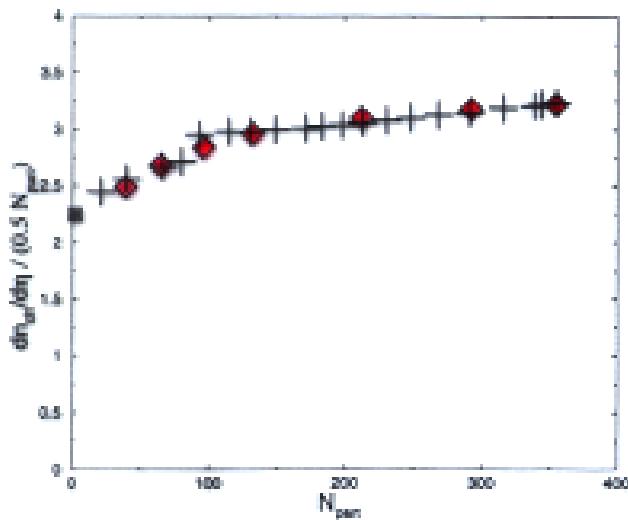
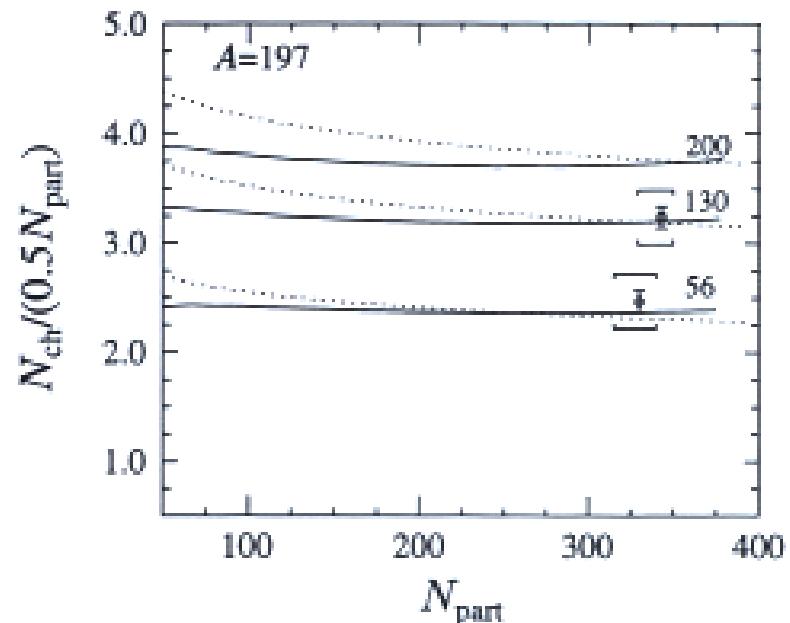
EVIDENCE FOR HARD SCATTERING ?

$$\frac{dN}{dy} = A \cdot N_{\text{part}} + B \cdot N_{\text{coll}}$$

HIJING



EKRT saturation



Kharzeev&Nardi

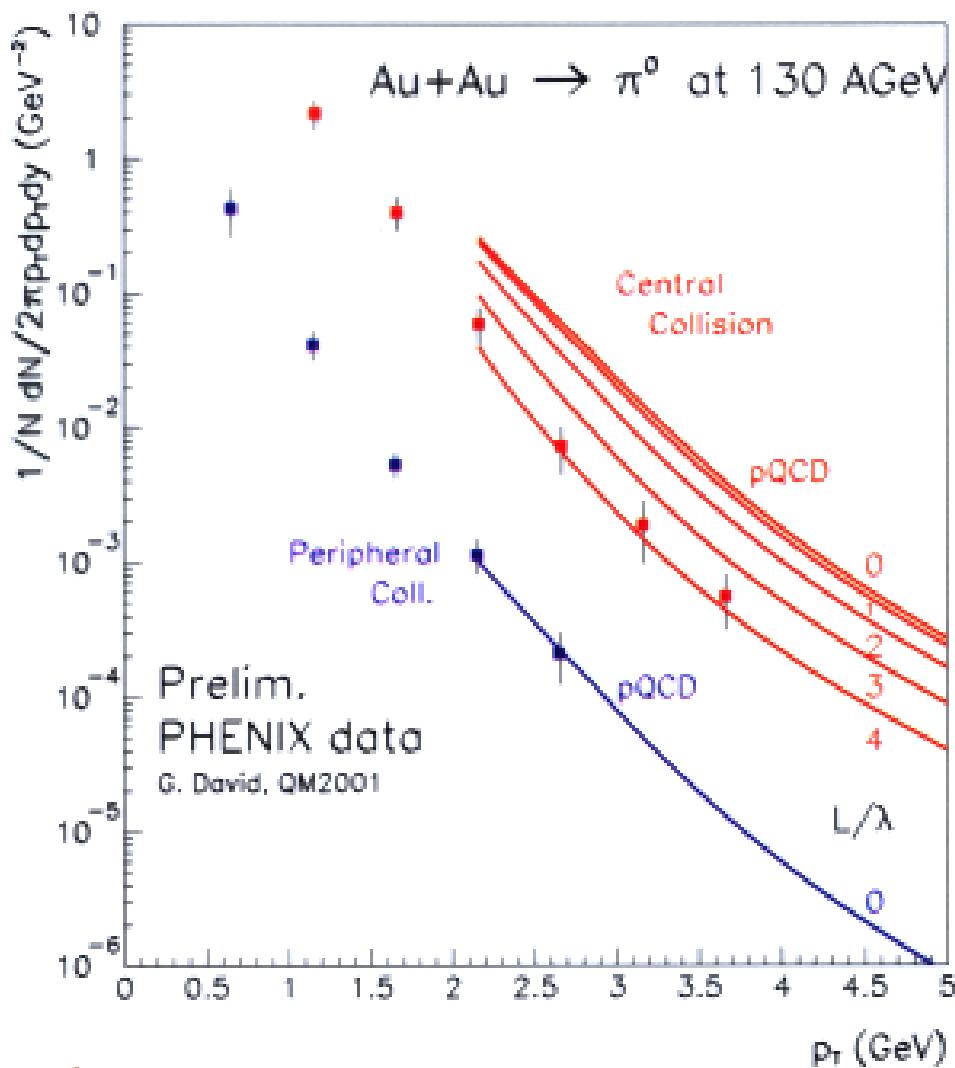
PHENIX

Jet quenching on hadron yields - 3

PHENIX prel. results at $\sqrt{s} = 130$ GeV [G. David's talk]

Periferial collisions (75-92 %; $< N_{coll} > = 5.5$)

Central collisions (10 %; $< N_{coll} > = 857$)



Factor 8-10 shift in central coll. \iff jet-quenching !!!!

INITIAL CONDITIONS

R. VENUGOPALAN

D. Son

(Y. Kovchegov, A. Dumitru)

IMAGINE

- VERY LARGE NUCLEI $A \rightarrow \infty$

AND/OR

VERY HIGH COLLISION ENERGY $s \rightarrow \infty$



A CONTROLLED PERTURBATIVE REGIME

$$\alpha_s(Q_s) \ll 1$$

WHERE QUESTIONS CAN BE ANSWERED ...

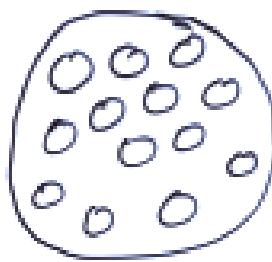
SATURATION

Which partons contribute dominantly to energy density?
Partons must collide to get freed.

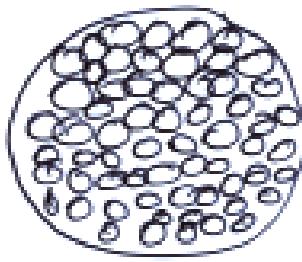
Optimum P_T given by saturation argt.



SMALL P_T



LARGER P_T



SATURATION

Growth of $\propto G(x, P_T^2)$ controlled by evolution equation. Enter non linear regime when

$$P_T^2 \propto \alpha_s \frac{A}{R^2} x f(x, P_T^2)$$

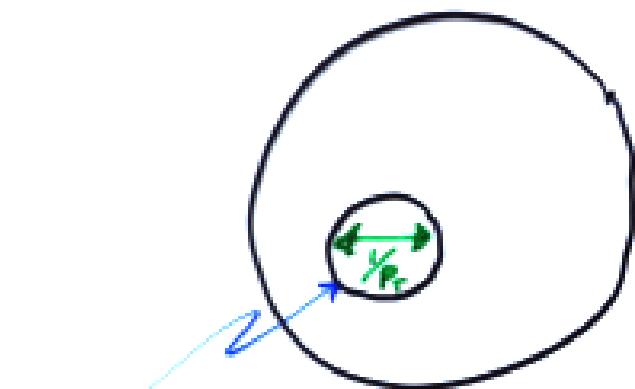
Then

$$\sigma \sim R^2 A x G$$

and

$$\frac{dN}{dy} = 2 A x G \quad \frac{dE_T}{dy} = 2 p_T A x G$$

At saturation



Quanta

$$\frac{A \times 6}{\pi R^2} \cdot \frac{\pi}{P_T^2} \sim \frac{1}{\alpha_s}$$

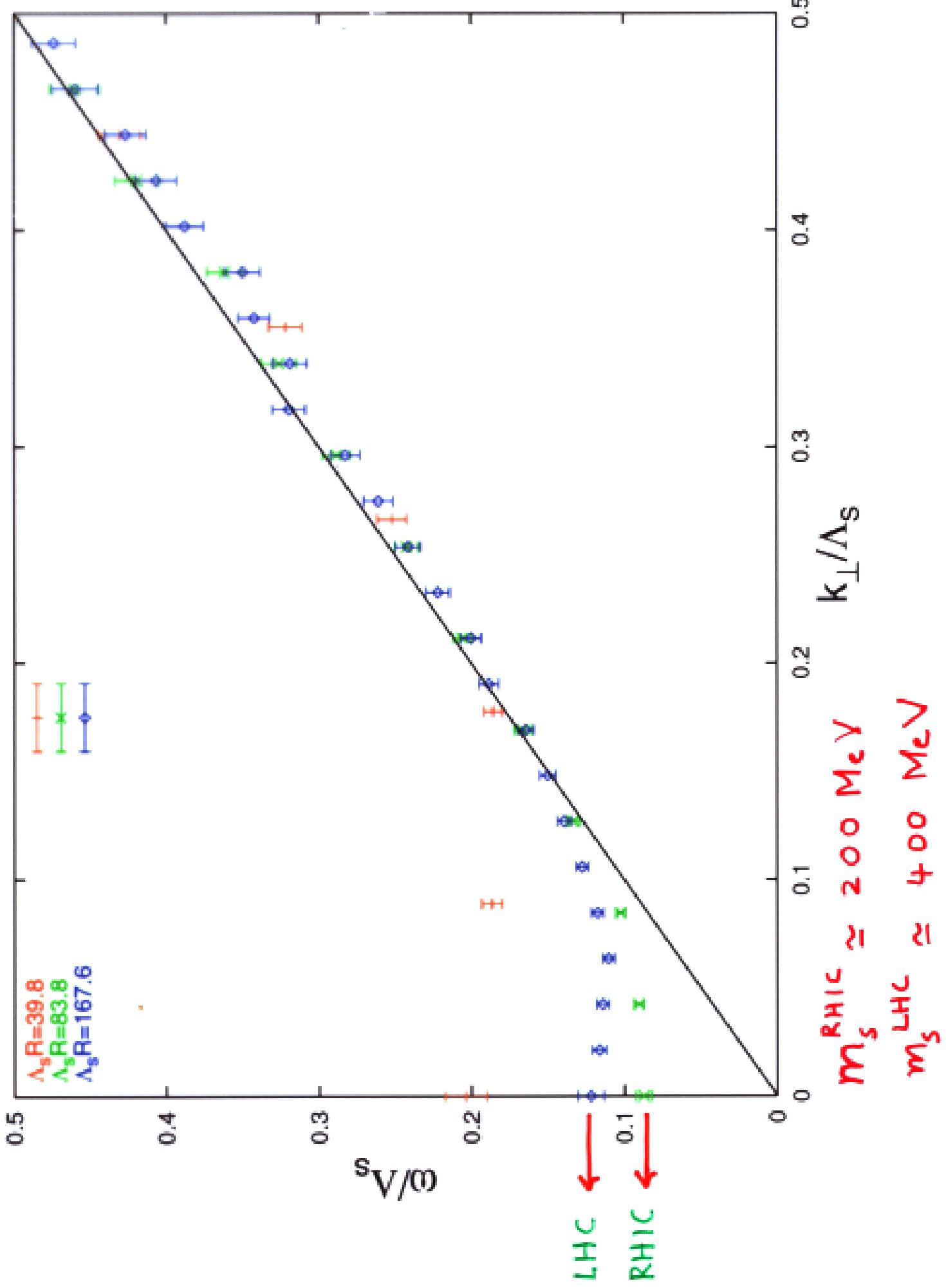
large nuclei (and high energy)

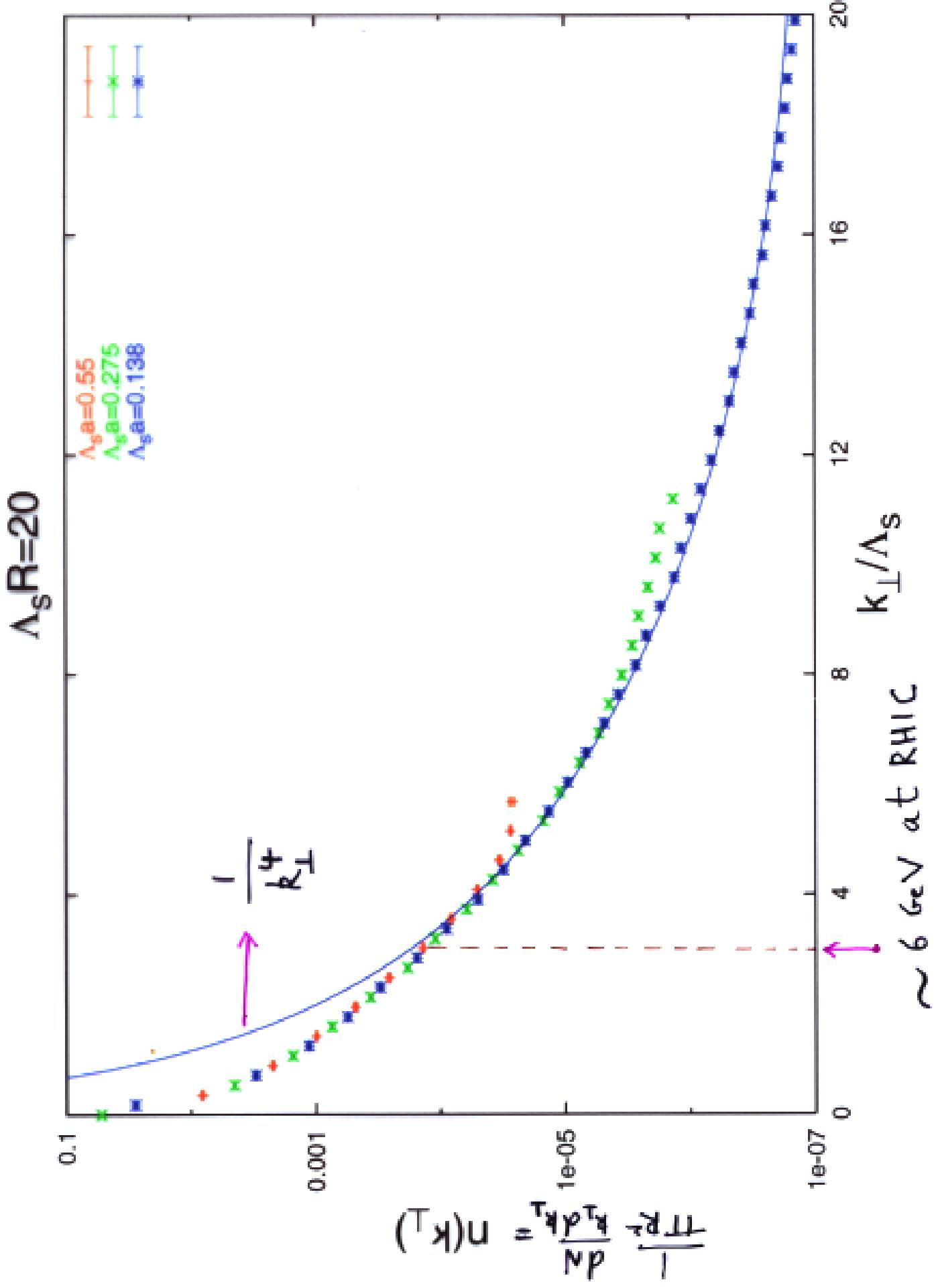
P_T^2 is large

$\alpha_s(P_T^2)$ is small

⇒ many quanta . Suggest classical approximation

(McLerran , Venugopalan)





Conclusions

- When $\alpha_s(Q_s) \ll 1$:

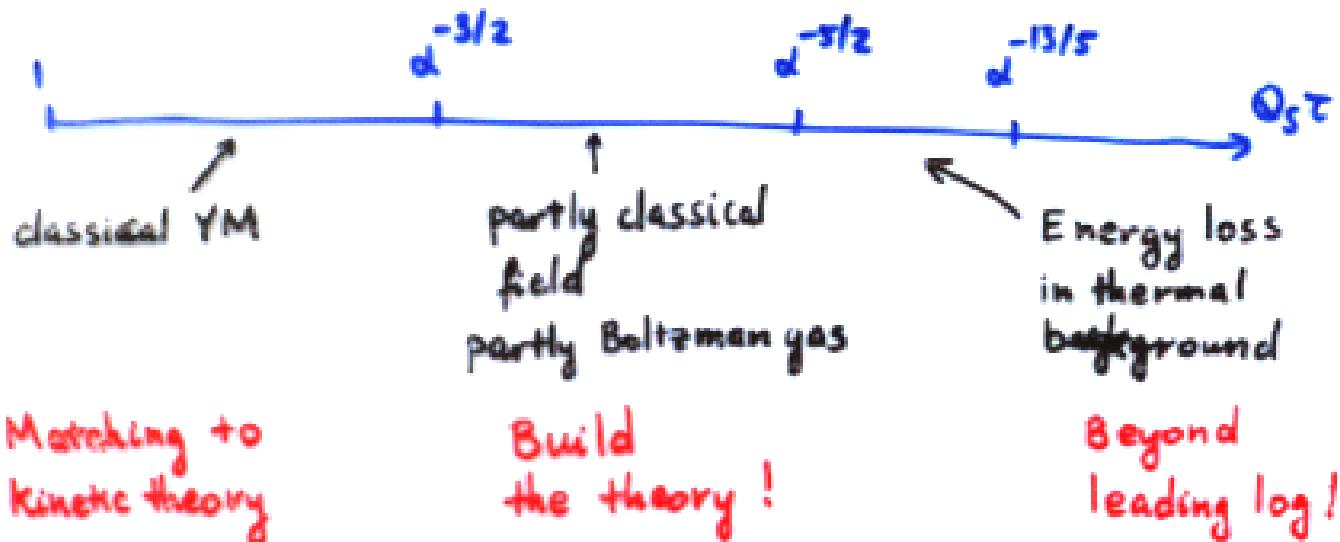
thermalization occurs

$$T \sim \alpha^{2/5} Q_s \quad \text{during} \quad \tau \sim \frac{1}{\alpha^{13/5} Q_s}$$

soft gluons thermalize first

$$\frac{N_{\text{final}}}{N_{\text{initial}}} \sim \frac{1}{\alpha^{2/5}}$$

- Three stages:



SPECIFIC OBSERVABLES

Fluctuations

V. Koch, N. Stephanov, A. Asakawa

Elliptic flow

P. Huovinen, D. Teaney, D. Nollier

Strangeness

K. Redlich, G-E. Brown

Dilepton

C. Gale, B. Kaempfer, R. Schneider
D. Srivastava, F. Gelis

J/4

J. Qiu, R. Thews, M. Diu, A. Capella

FLUCTUATIONS

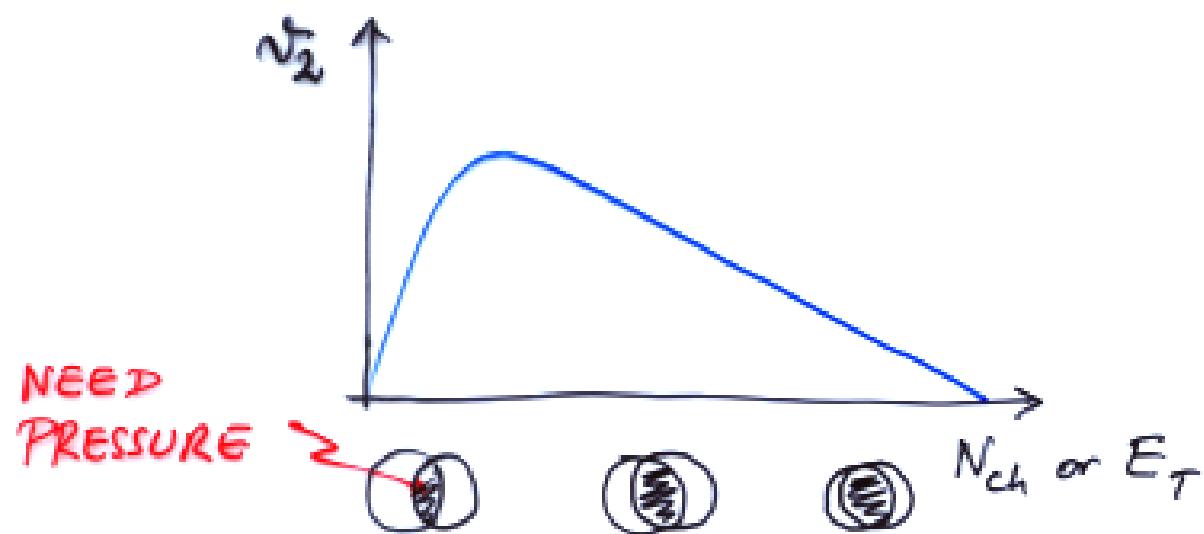
- "Interesting" sources of fluctuations
(near phase transition (Gavin, Hama),
DCC, ...)
at large or small ϕ_T .
- Fluctuations in conserved
Quantities (Koch, Asakawa, Stephanov)
(NB. Related to correlator
of conserved current)
- Related Work: "balance function"
(S. Pratt)

In Progress . . .

"Absence of evidence is
not evidence of absence"

V. Koch

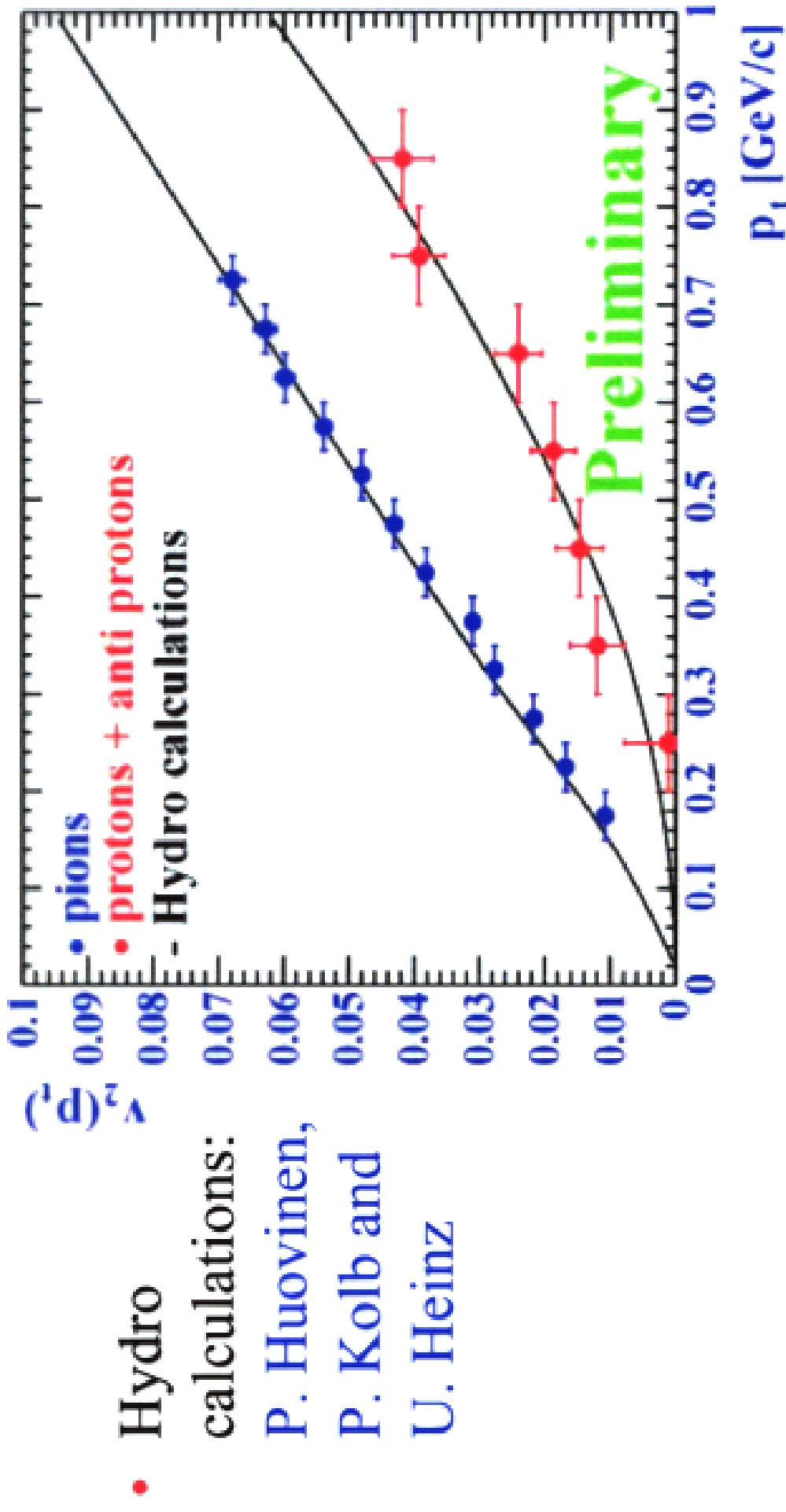
ELLIPTIC FLOW



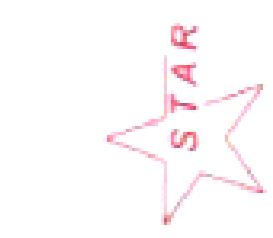
- Linear decrease with centrality predicted by hydro (J.-Y. Ollitrault, 92)
- P_T dependence of v_2
 - effect of the mass
 - decrease at $P_T > 2 \text{ GeV}$
(predicted by X.N. Wang 09/00)
- QGP influence unclear
- Sensitivity to early times (?)



A Hydro view of the world

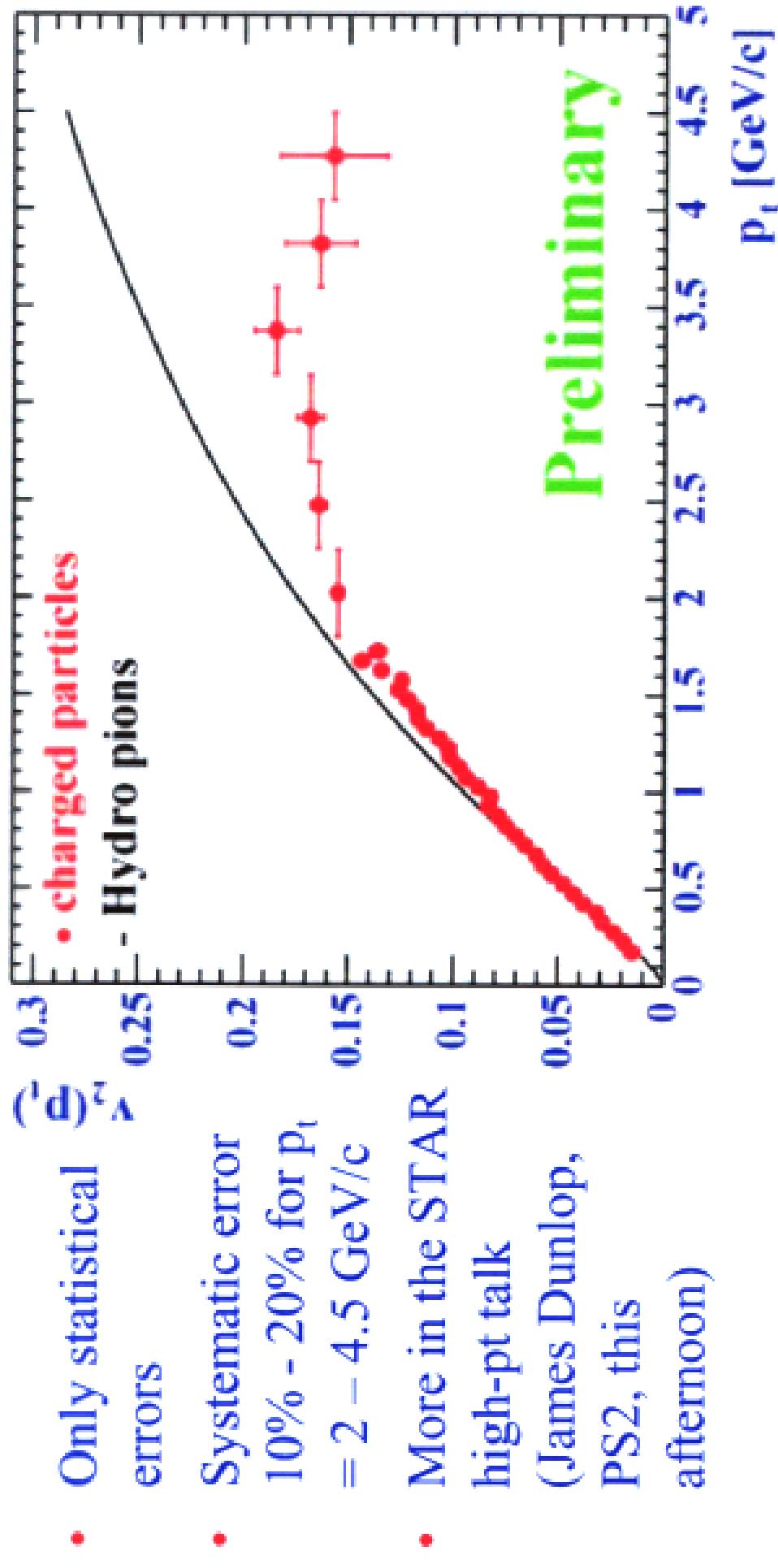


- Hydro calculations:
 - P. Huovinen,
 - P. Kolb and
 - U. Heinz



Charged particle anisotropy

$0 < p_t < 4.5 \text{ GeV}/c$



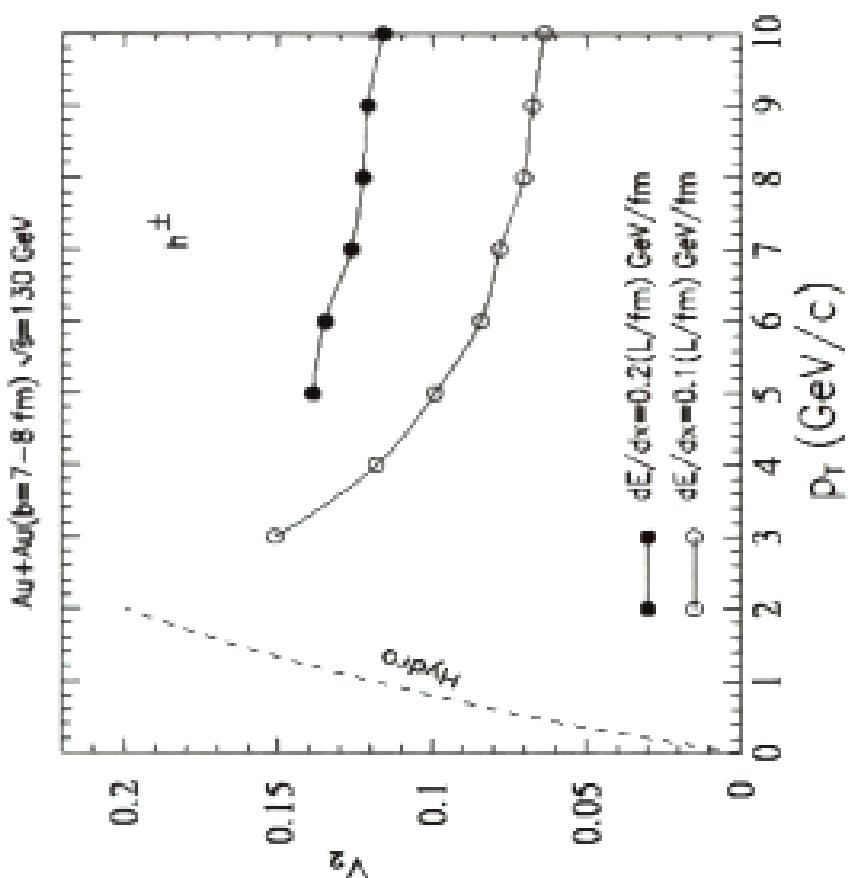
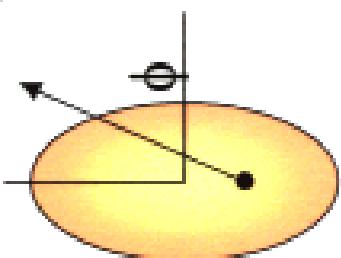
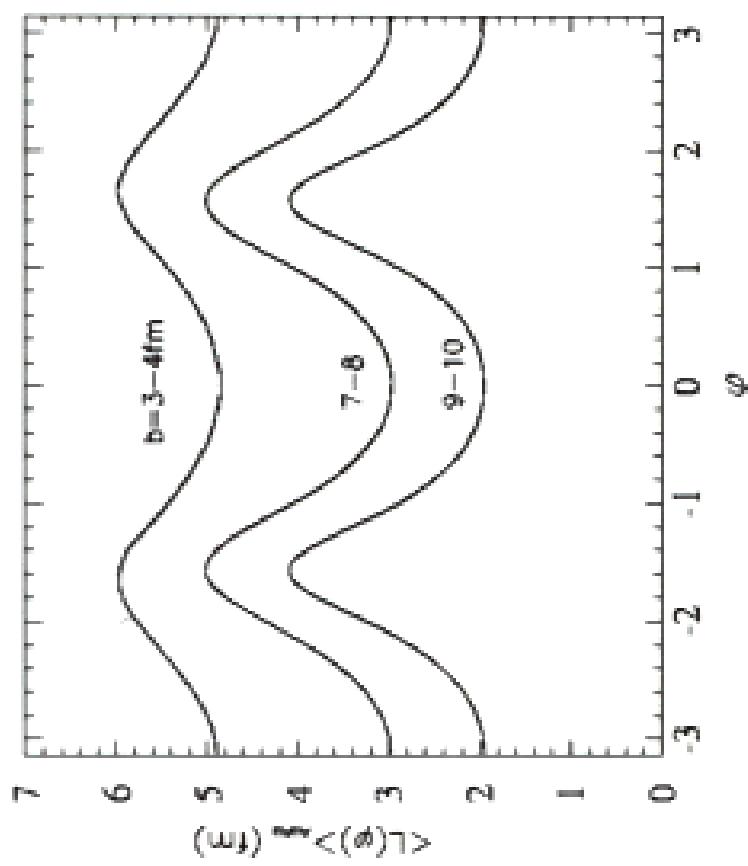
- Only statistical errors

- Systematic error
10% - 20% for $p_t = 2 - 4.5 \text{ GeV}/c$

- More in the STAR high-pt talk
(James Dunlop,
PS2, this afternoon)

Azimuthal Anisotropy

Anisotropy in geometry:



Anisotropy in jet quenching

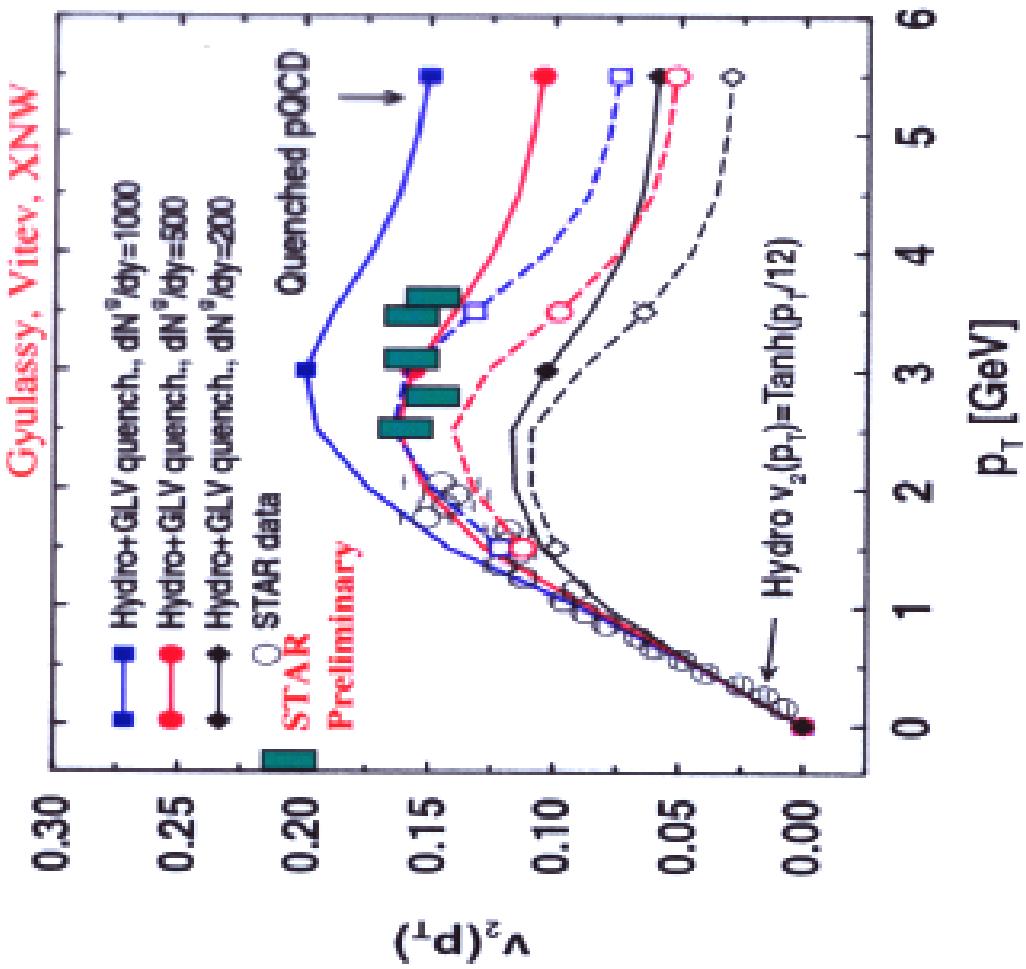
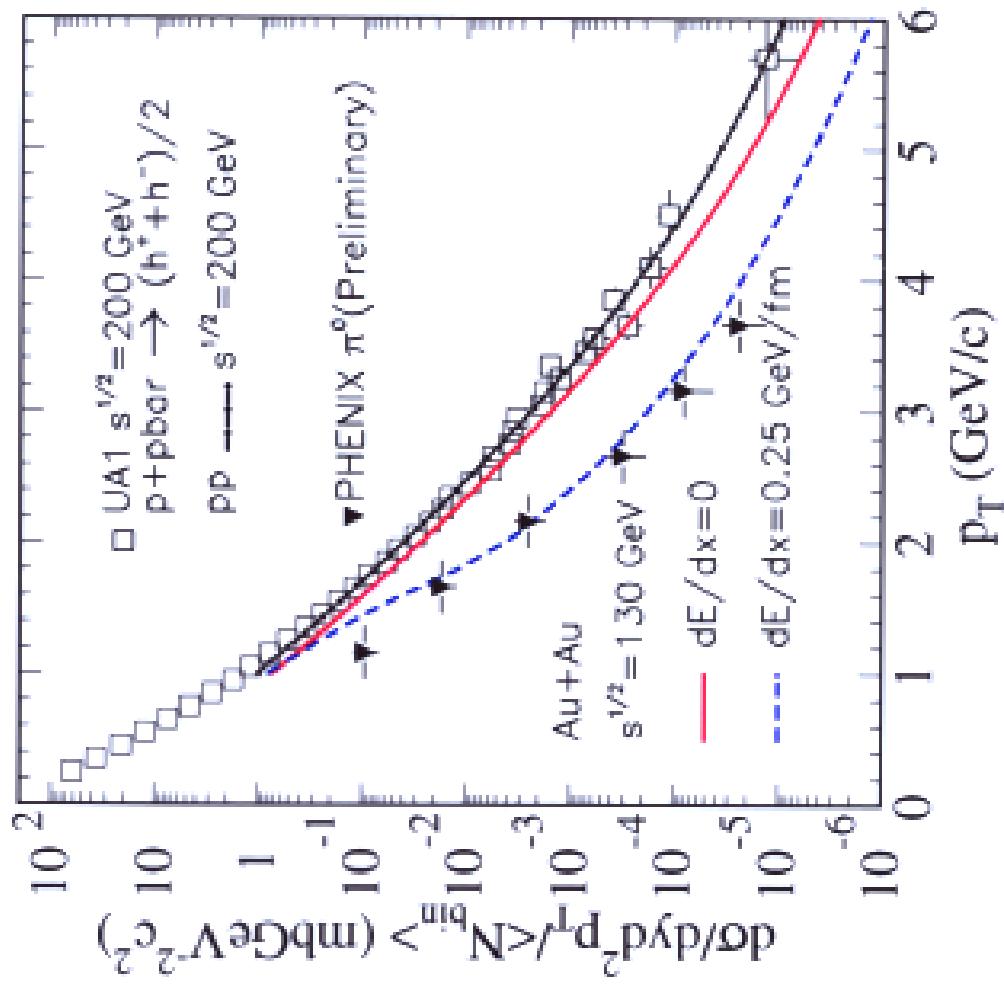
nucl-th/0009019

QM₂₀₀₁

Probes of initial parton density

$v_2(p_T)$ at large p_T is very sensitive to initial parton density

$$\Delta E \propto \rho_g(\tau_0)$$



STRANGENESS

- strangeness enhancement/
suppression
(K. REPLICH)
- how can we understand
chemical equilibrium?
 - role of n-body processes (Rapp)
 $p\bar{p} \leftrightarrow n\pi$
 $\bar{\gamma} + p \leftrightarrow n, \pi + n_2 \kappa$ (Greiner)
 - also, dropping mass (G.E. Brown)
- threshold for onset of
strangeness enhancement

Conclusions

SPS data are consistent with the predictions of QGP

However: these predictions are not a unique signal for deconfinement:

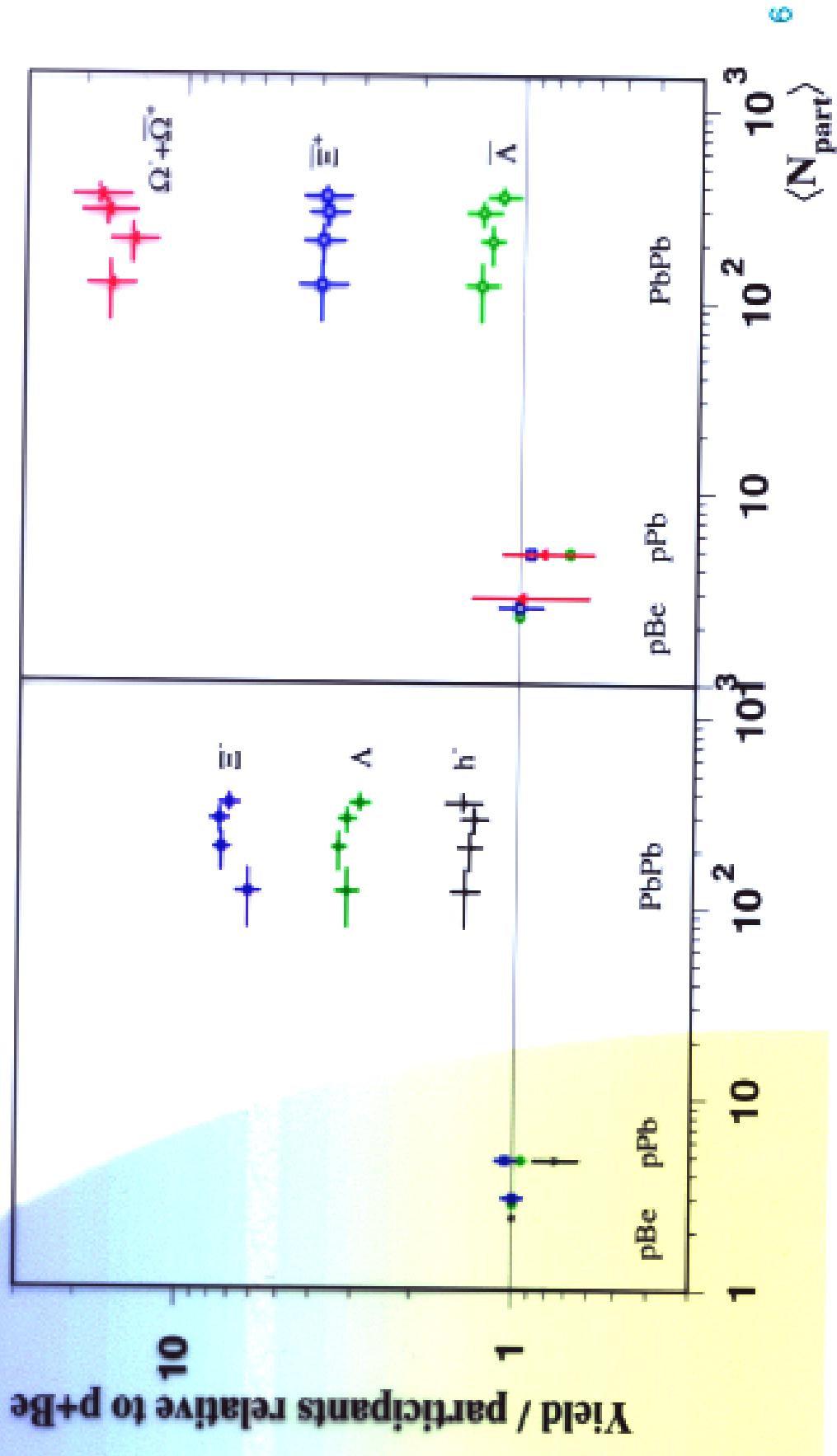
- Chemical equilibrium population of hadronic yields observed in A-A collisions from SIS, AGS, SPS to RHIC

- Strangeness enhancement already appears in p-A
 - Enhancement (K^+ / π^+) from p-A to A-A collisions increases with decreasing \sqrt{s}
- the above also expected for multistrange baryons?

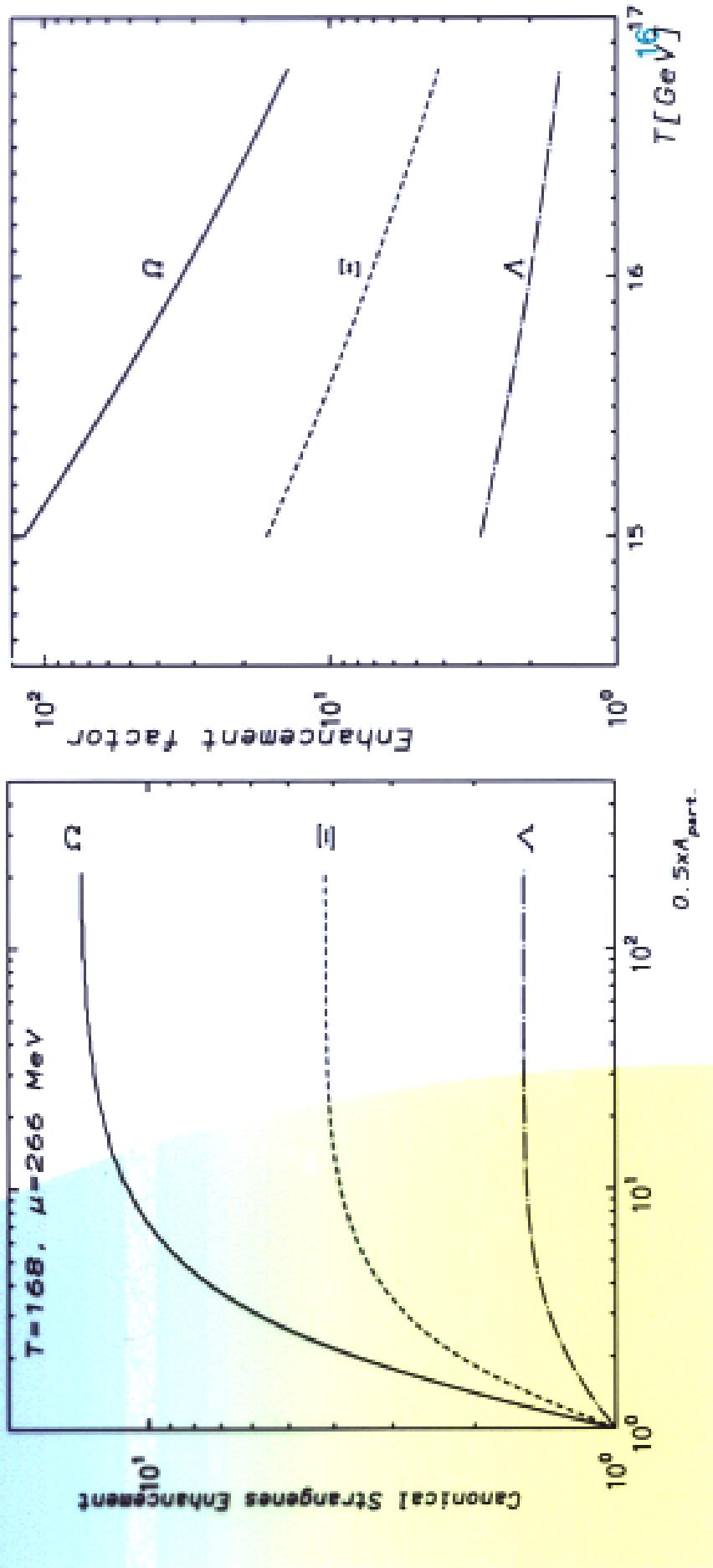
- Suppression of K^+ / π^+ (NA49 4 π data) from 40 => 158 AGeV Pb-Pb collisions could signal new dynamics

(Multi) Strange Baryons Enhancement

WA97

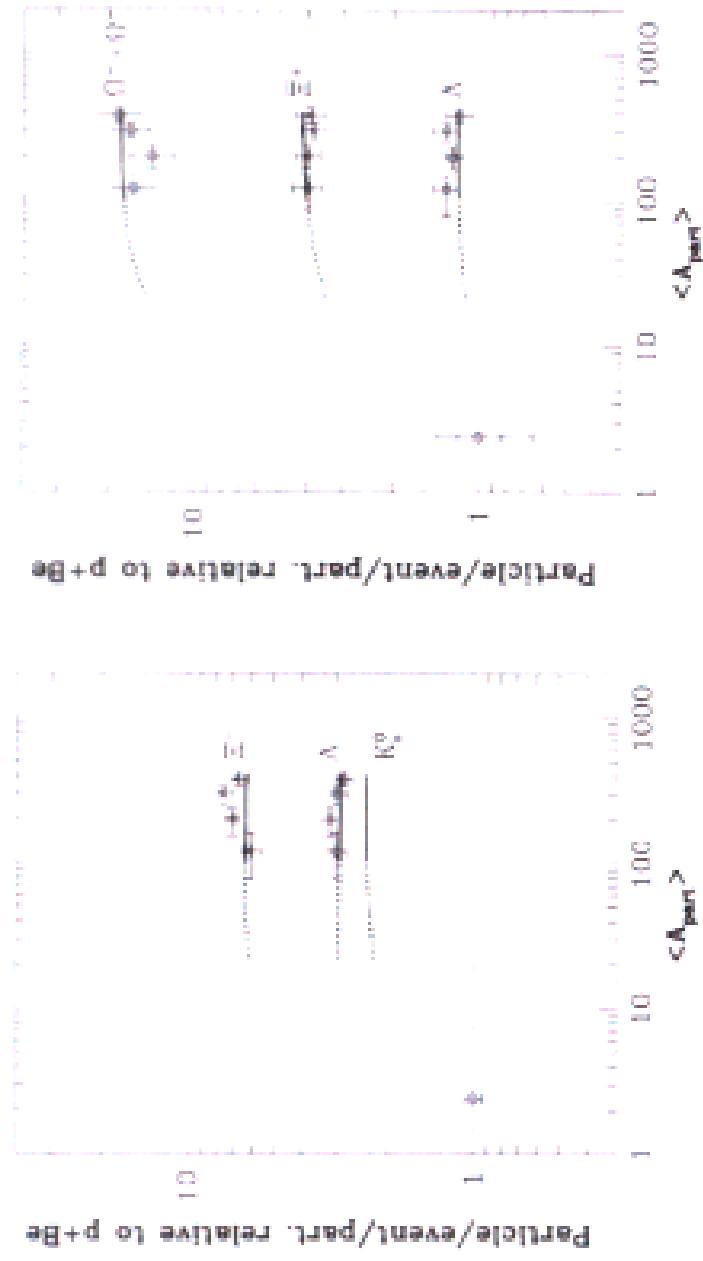


Statistical Model – Centrality Dependence approaching asymptotic – grand canonical limit

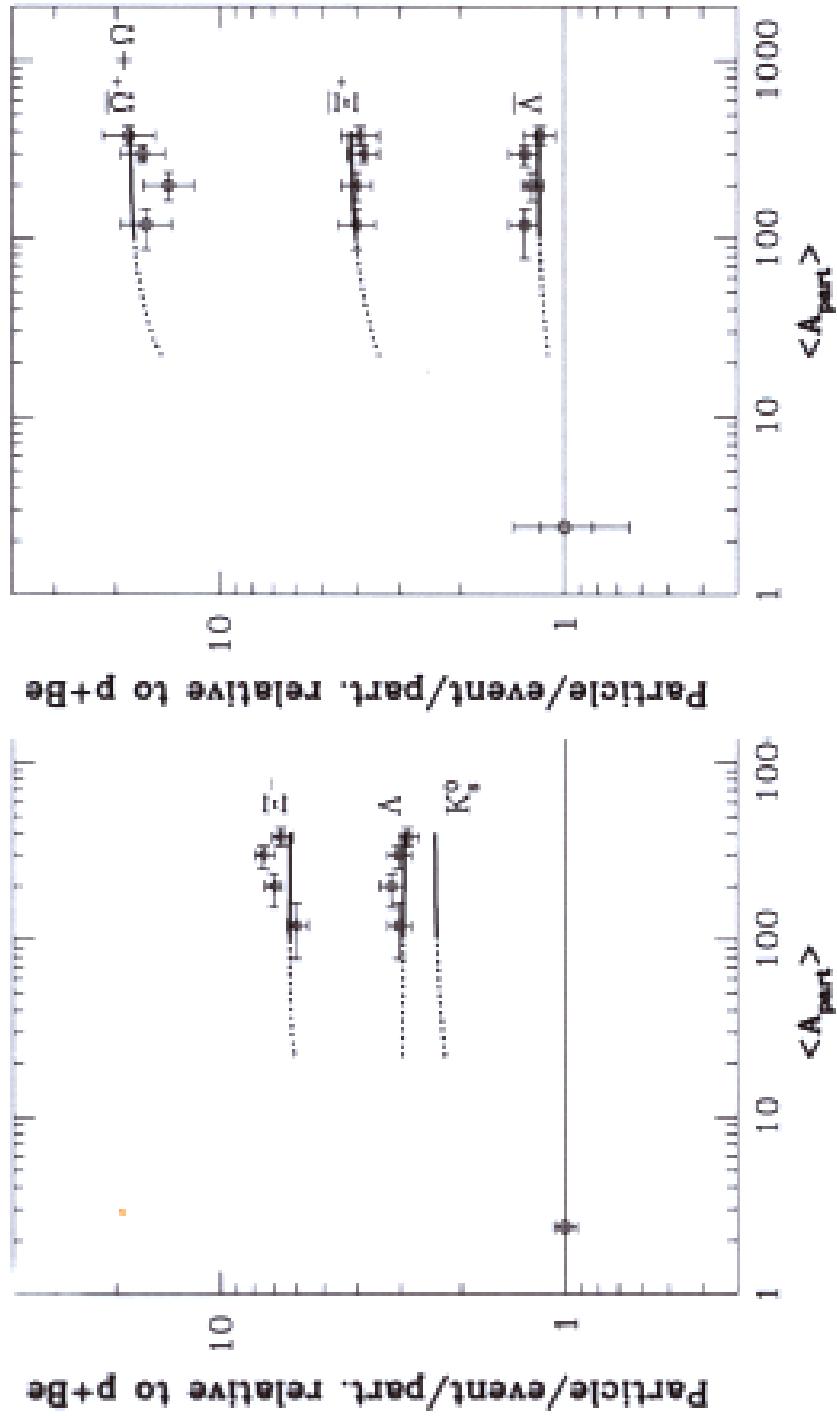


Statistical canonical model

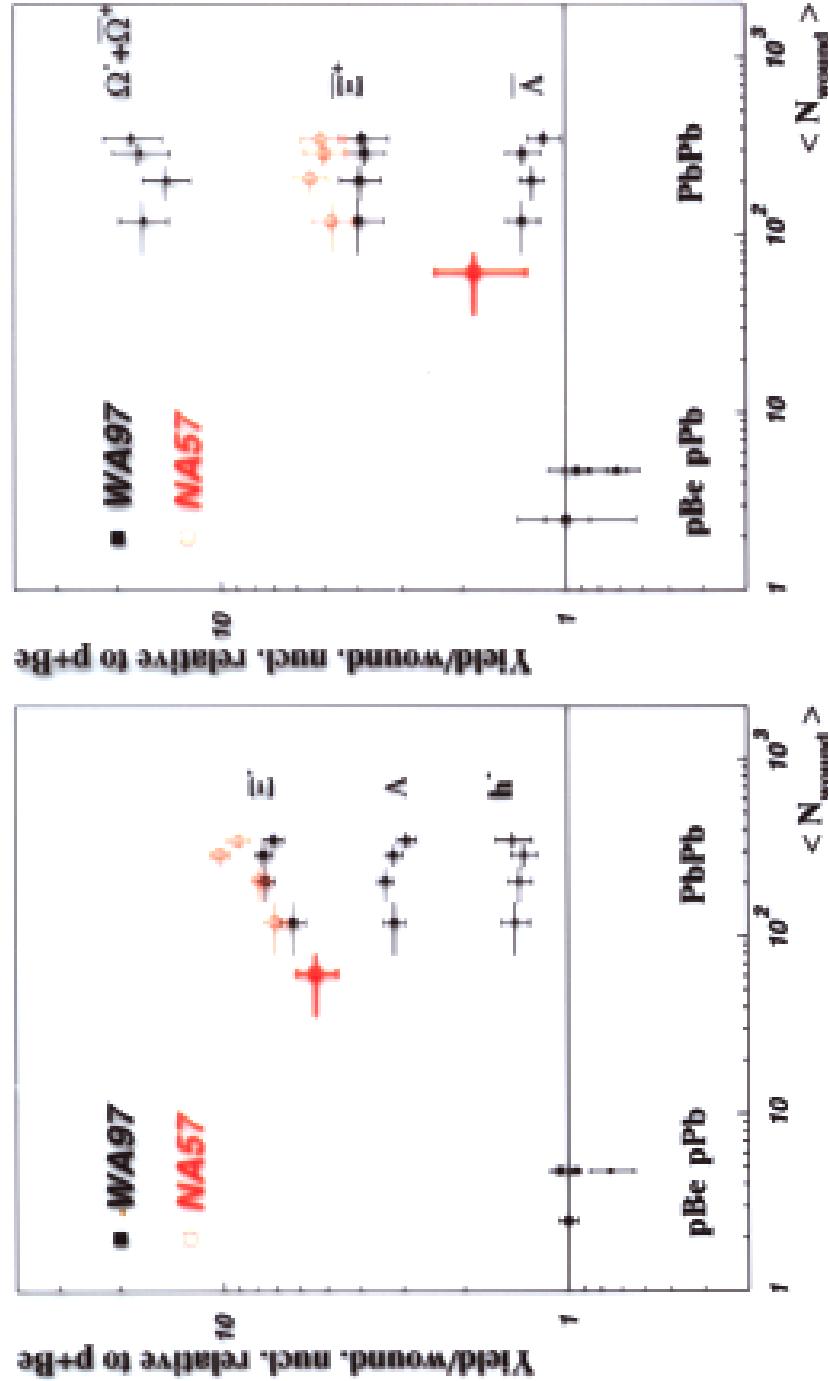
S. Hamieh, K. Redlich and A. Tounsi hep-ph/0006024



- Reproduces WA97 hyperon data
- Predicts enhancements ~saturated down to $N_{wound}=20$



Yields per participant



- Yield per N_{wound} rises from $\langle N_{\text{wound}} \rangle = 62 \rightarrow 121$ both for Ξ^- and for Ξ^+
 - 2.6 for Ξ^+ (3.5σ effect)

PHOTONS - DILEPTONS

Reviewed by C. Gale

Low mass dileptons (Schneider, Kaempfer)

Some progress but new precision data are waited

Direct photons

(QCD calculation of the rate at 2 loop order (F. Gelis))

When included in hydron evolution, fit WA98 - But inconclusive. (D. Svirastava)

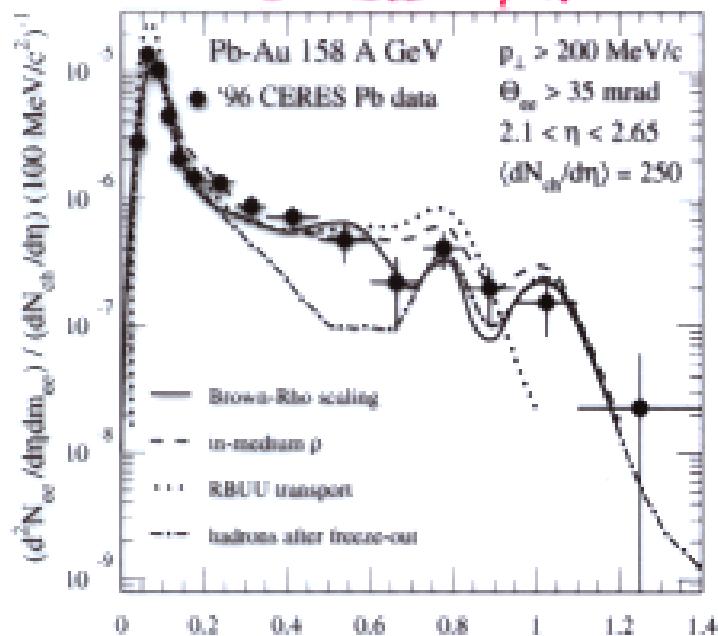
Intermediate mass dileptons

Role of thermal contributions

• (Competing with open charm)

Dileptons: low mass

I. TICHLIYA, 99

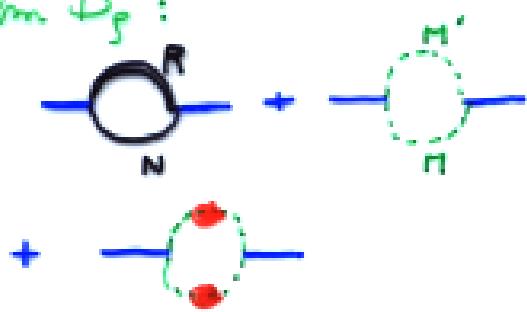


BR: BROWN, RHO, LI 1992

TRANSPORT: V. KOCH, 1999

CASSIS & BRATTKE-DIERK 98

$\text{dm } D_F :$



FRIMAN, PIRNER 92

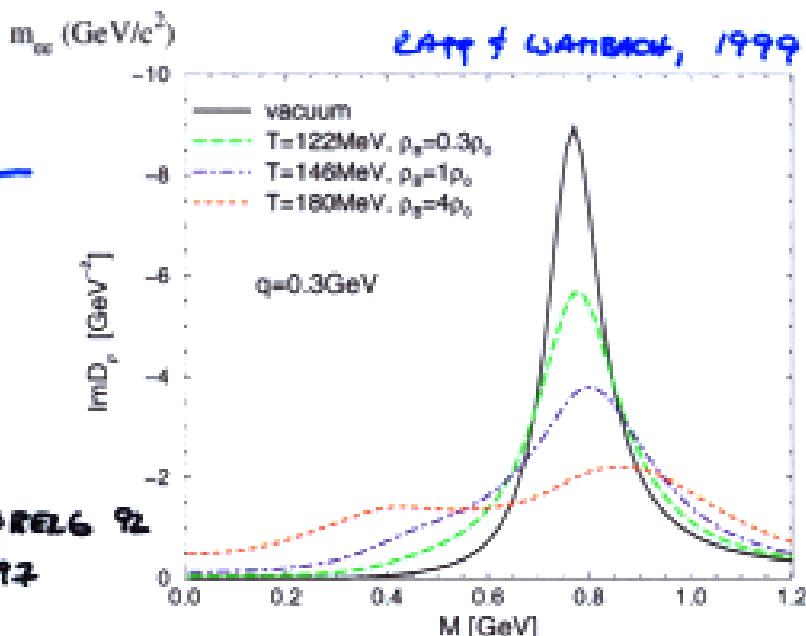
HERDANN, FRIMAN, NÖTENHELS 92

RAPP, CHAP-FRAY, WAMUTH 92

PETERS et al. 98

SIBIRTSEV, ORSING 98

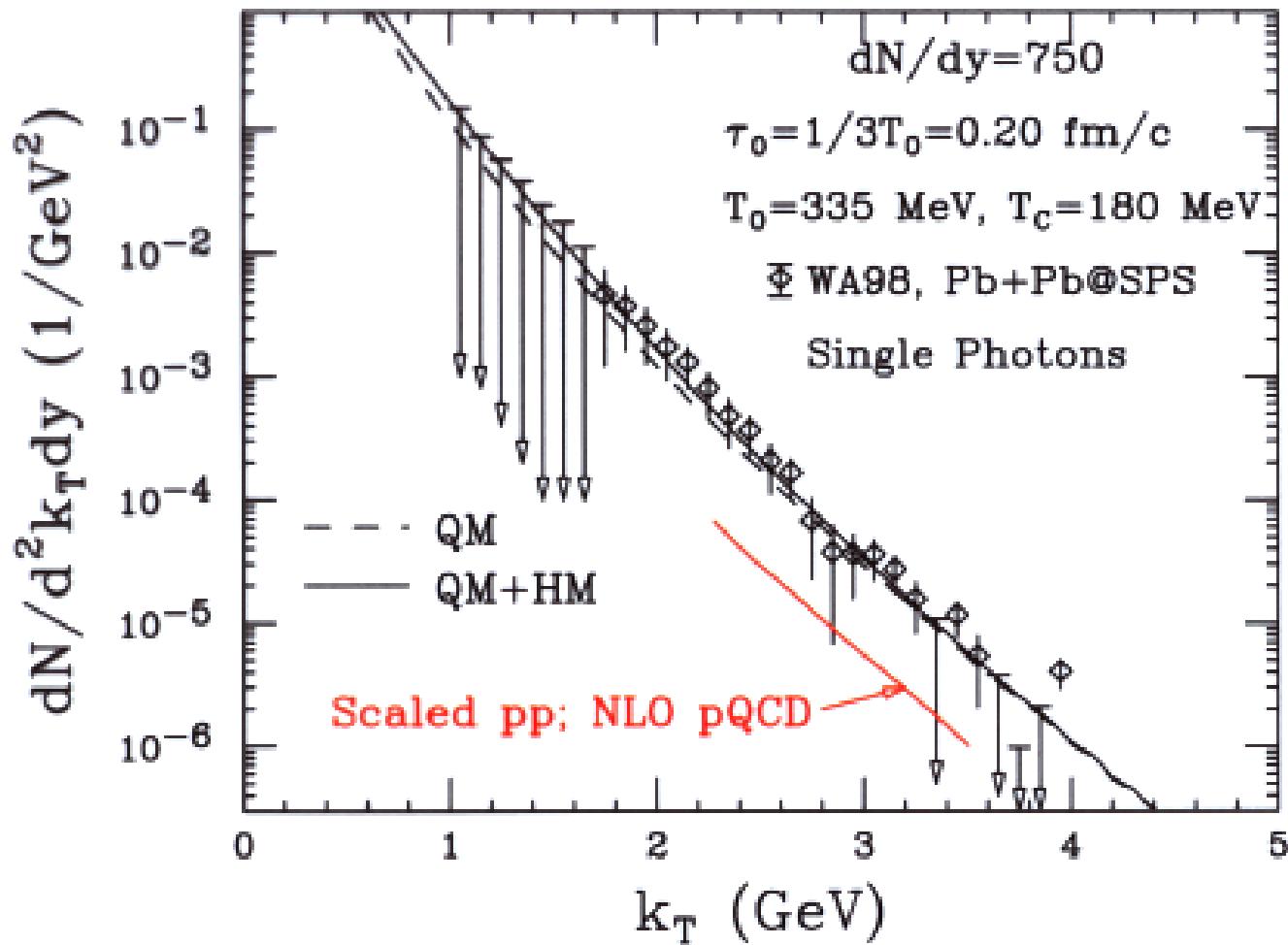
ELETSKY, JAFFR, KAPUSTIN 98



• RA DATA

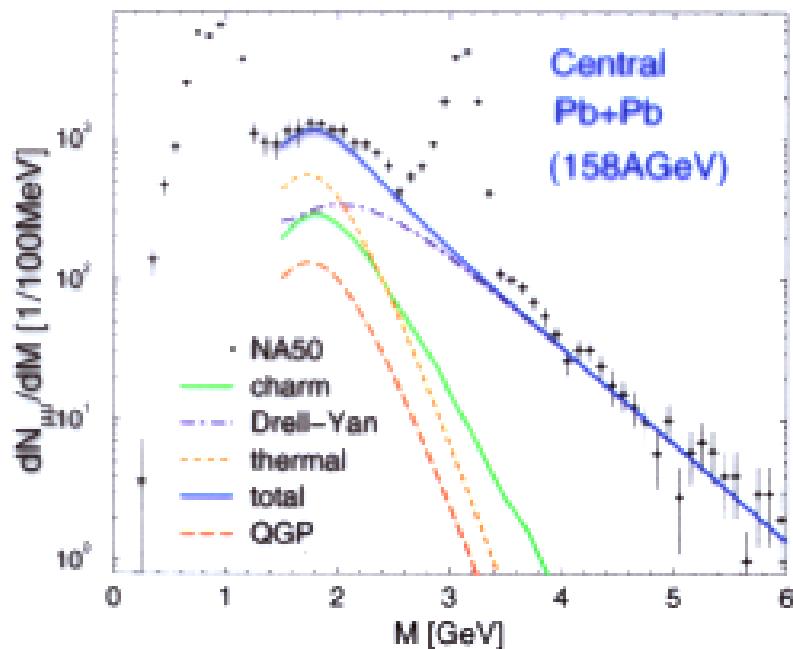
• p_T dependence $\propto 1/p_T^2$
excess

D.-K. SRIWASTAVA & B. SINGH, 2000

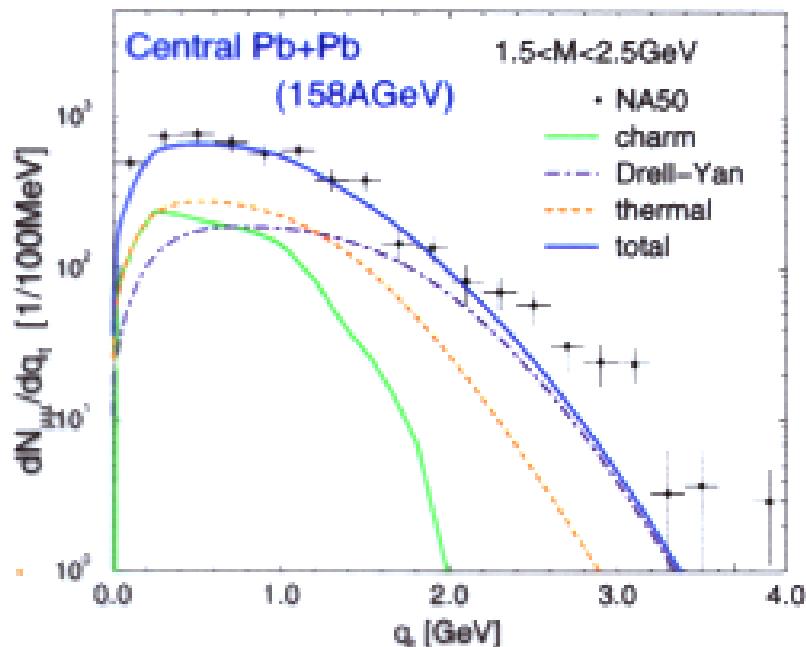


CONTAINS THE HIGHER ORDER α_s^2
RESULTS OF AULENAUKE, GÉVÍS ET AL.

Intermediate mass dileptons (II)



R. Rapp & E. Shuryak,
PHYS. LETT. B473, 13
(2000).

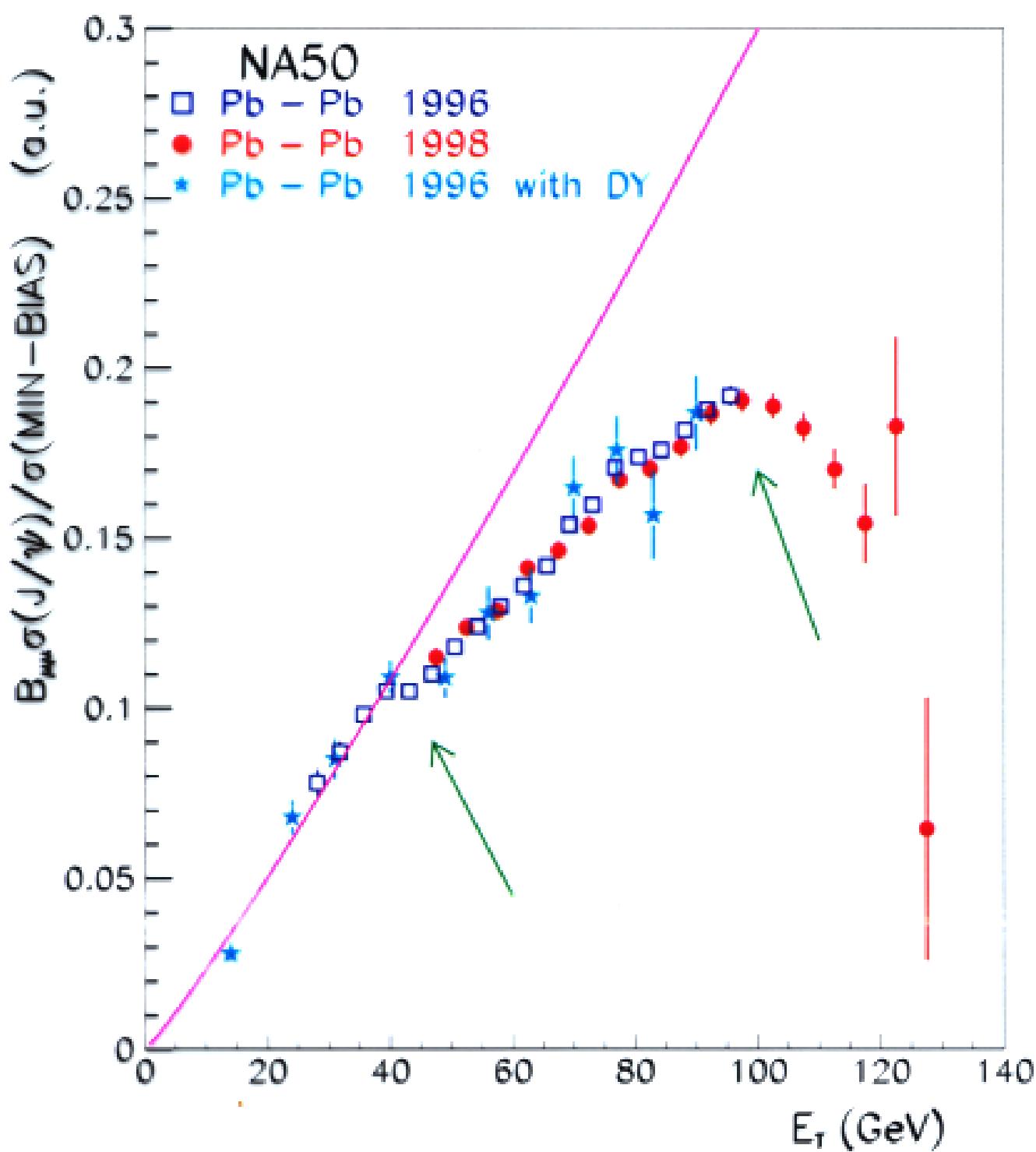


THE INTERMEDIATE-MASS REGION "IS FILLED IN"
BY THE "THERMAL" CONTRIBUTION.

J/ψ

- New mechanism for "nuclear absorption" (J.Qiu)
- Role of transverse energy fluctuations (M.Dinh, A.Capella)
- J/ψ enhancement at RHIC! (R.L.Thews)

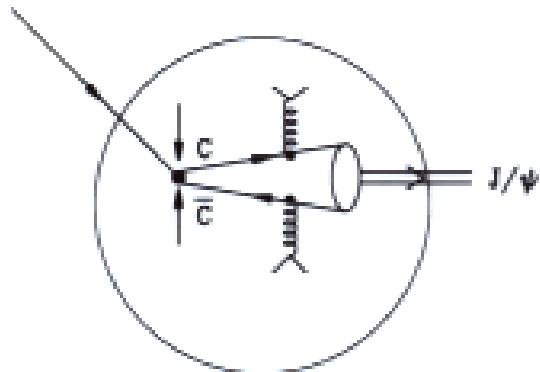
ψ /Minimum Bias as a function of E_T



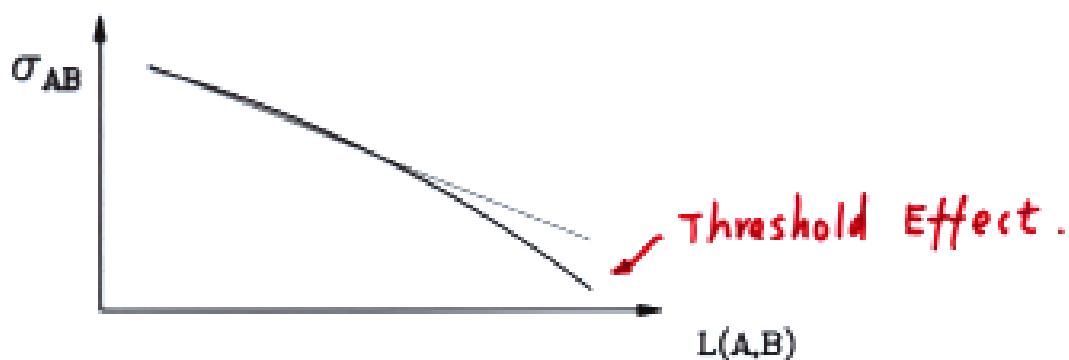
Solid line: Absorption Model with $\sigma_{abs} = 6.4 \pm 0.8 \text{ mb}$
as obtained from fit to p-A and S-U data (NA38 +
NA51) with full calculation

Pattern exhibits 2 "accidents"

NEW SUPPRESSION MECHANISM

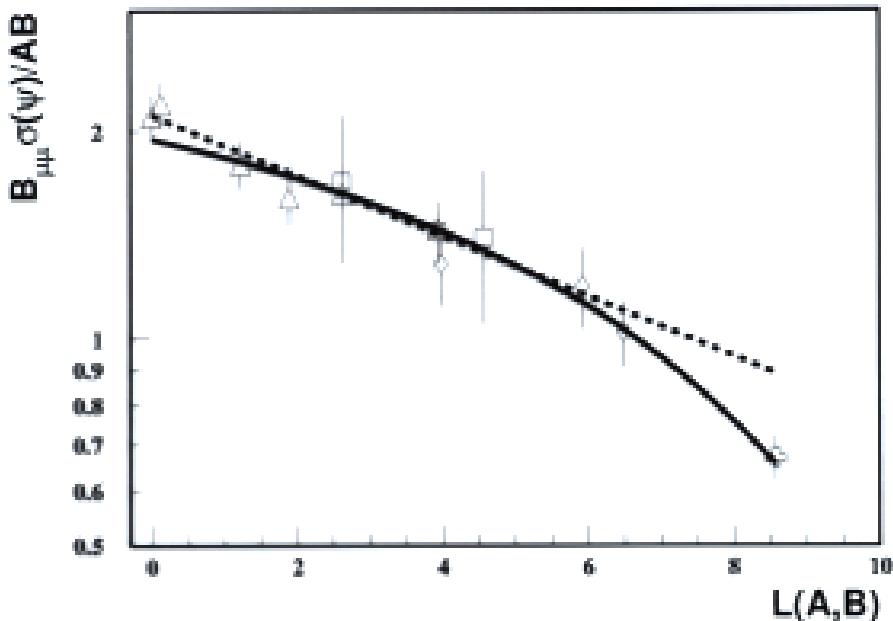


- J/ψ are not produced at the point of hard collision
⇒ partonic $c\bar{c}$ states going through medium
- Multiple scattering with nuclear medium increase the invariant mass of the $c\bar{c}$ pairs
⇒ push some $c\bar{c}$ pairs over the open charm threshold
⇒ “suppress” the production of J/ψ (see figure)
- The suppression rate depends on
 - Gain of invariant mass per medium length: ϵ
 - Functional form of the transition probability:
 $F_{[c\bar{c}]\rightarrow J/\psi}(m_{c\bar{c}}^2)$
 - Functional form of the $c\bar{c}$ cross section: $\frac{d\sigma_{AB\rightarrow c\bar{c}}}{dm_{c\bar{c}}^2}$
- Expect a non-linear behavior on the semi-log plot

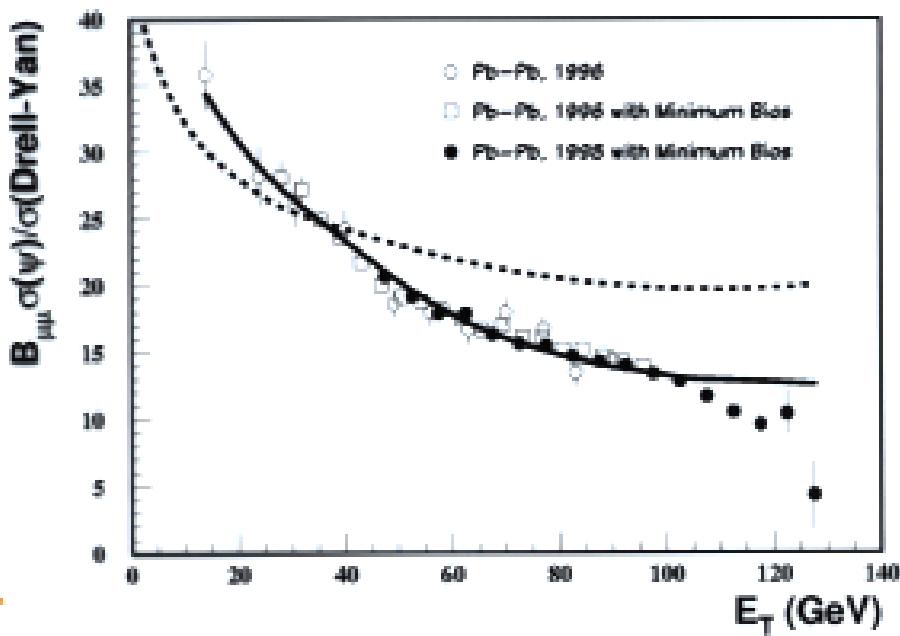


COMPARISON WITH J/ψ SUPPRESSION DATA*

- J/ψ production as a function of effective medium length:



- Ratio of J/ψ over Drell-Yan as a function of E_T :



* Data from Phys. Lett. B410, 337 (1997); B477, 28 (2000)

Variations of $\langle p_T^2 \rangle$

Assumptions

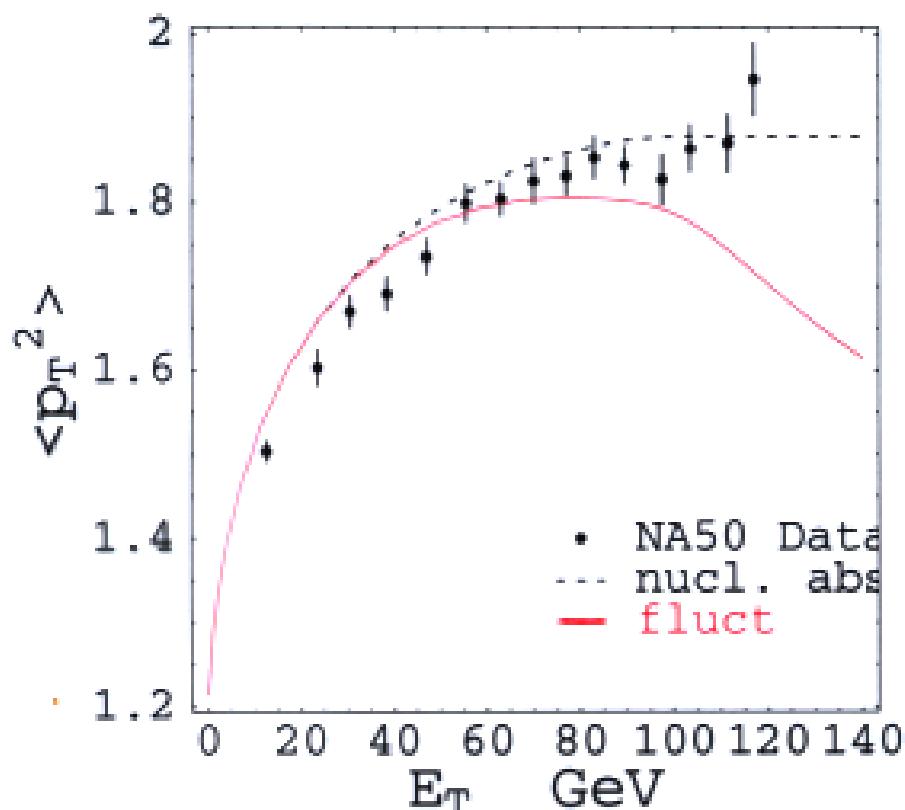
- Initial state scattering

$$\langle p_T^2 \rangle_{AB} = \langle p_T^2 \rangle_{pp} + a \langle L \rangle$$

length of crossed matter \leftrightarrow

NA50, CERN-EP-2000-141 Nov 2, 2000
Kharzeev *et al*, Phys. Lett. **B405** (1997) 14

- Anomalous suppression taken p_T -independent



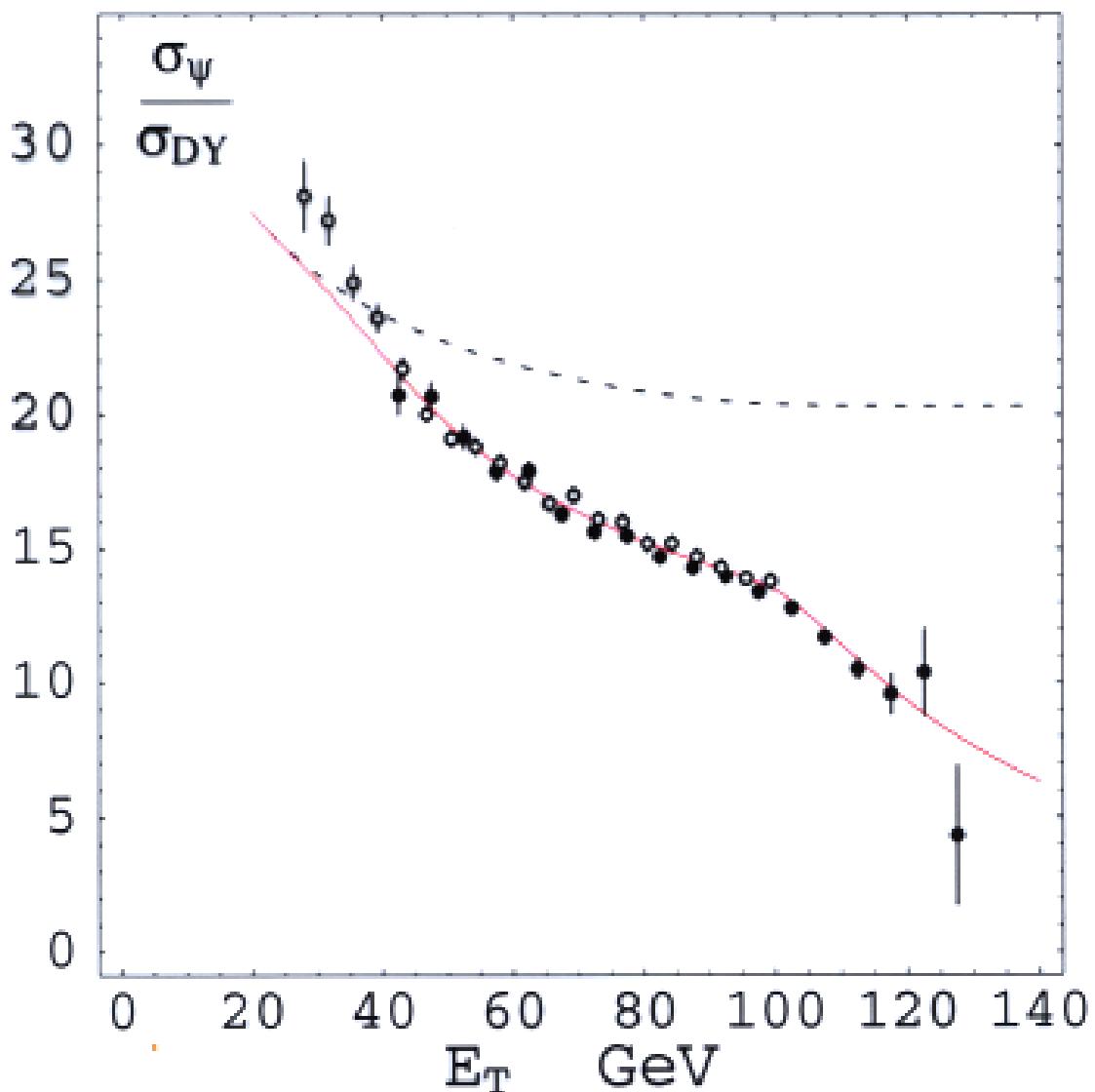
- Possible improvement

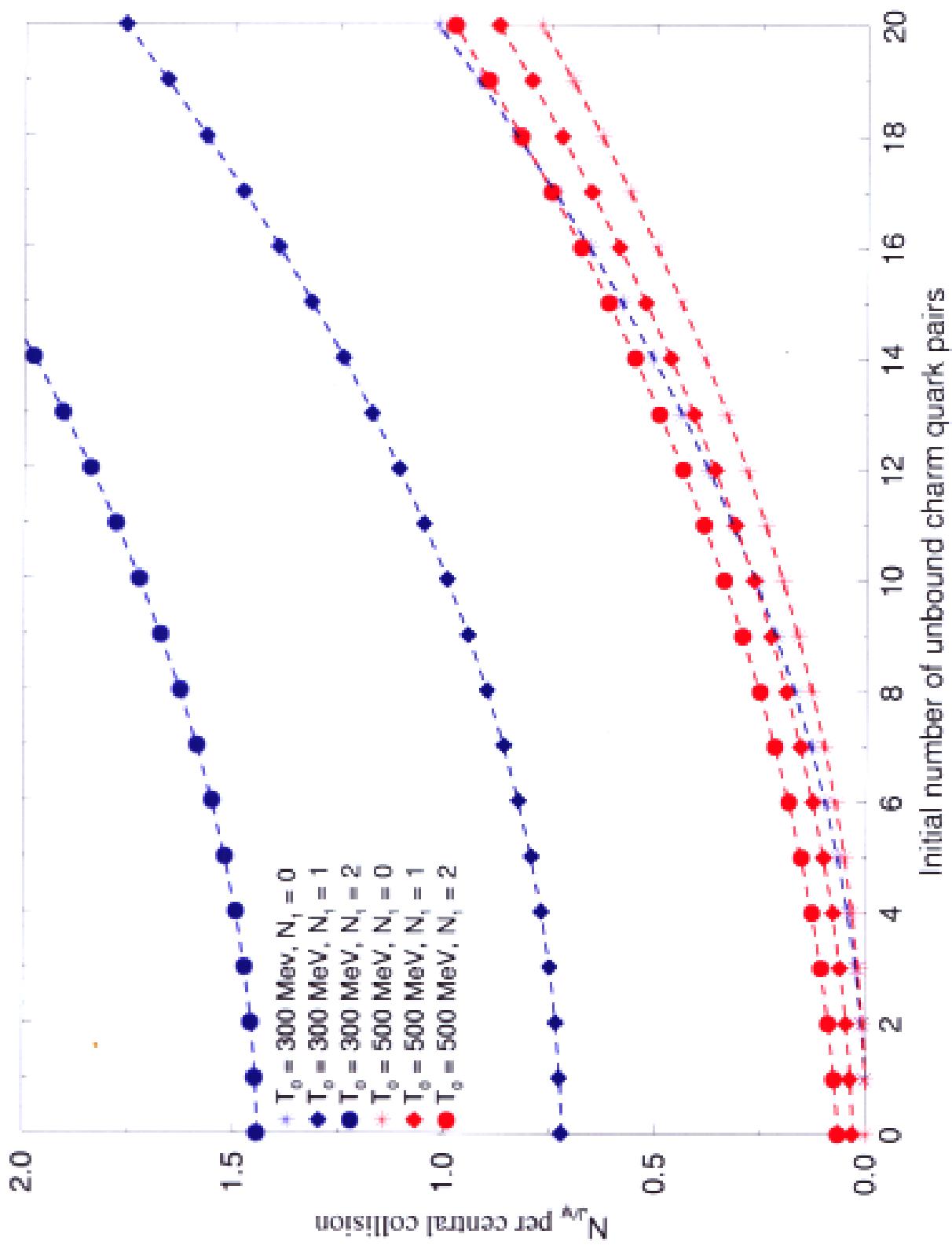
consider less suppression at high p_T

Fit to NA50 Data (2)

[M. Dinh]

Two thresholds or gradual suppression





Formation Mechanism Energy Dependence

